

# What is Geodynamics?

Geodynamics is a subfield of geophysics dealing with dynamics of the Earth and Planets.

It applies physics, chemistry and mathematics to the understanding of geologic phenomena such as mantle convection, seafloor spreading, mountain building, volcanoes, earthquakes, faulting and so on.

# What is special in Geodynamics?

As a scientific discipline, geodynamics is distinguished from other Earth Science disciplines in that it starts from fundamental physical principles to interpret and predict Earth's behavior, rather than working backwards from observations.

Moreover, geodynamics explicitly treats Earth's complex material properties, in addition to its dynamics.

# Computational geodynamics

Lectures -- morning, Tutorial-Training -- afternoon

13.03 15.00 Lecture by Prof. Trond Torsvik in GFZ

14.03 Visit to the Geodynamic Modeling Section at GFZ

Detailed program and recommended literature at  
<http://www.dynamicearth.de/fortgeo>

“Everything should be made as simple as possible, but not simpler.”

A. Einstein

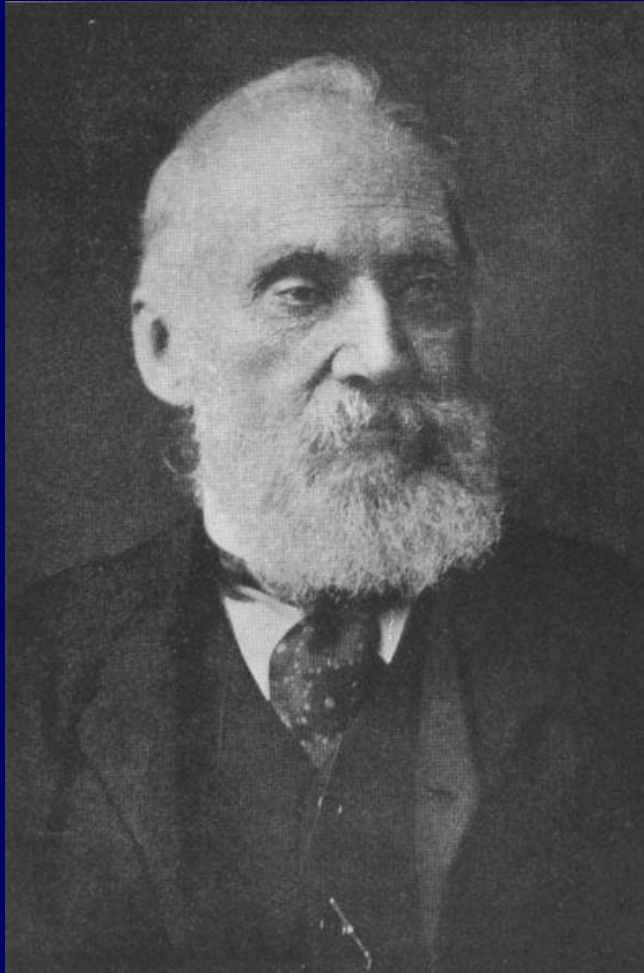
# Introduction: historical notes and overview of major challenges in solid Earth dynamics

## Outline

- Beginning of geodynamics: Lord Kelvin's error
- Why plate tectonics at the Earth?
- Key plate-tectonic challenges and mysteries
- Beyond the plate tectonics

# Lord Kelvin error

1862- age of the Earth is between 20 and 400 Mln yrs



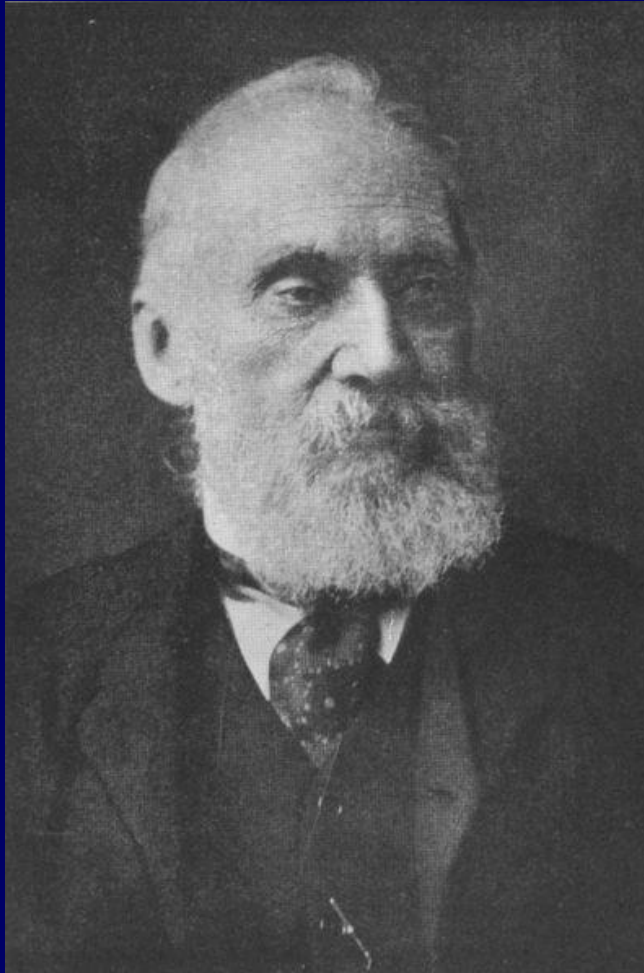
$$\frac{\partial T}{\partial t} = \kappa \frac{\partial^2 T}{\partial z^2}$$

$\kappa = \lambda/\rho C$  -thermal diffusivity

William Thomson, Lord Kelvin (1824–1907)

# Lord Kelvin error

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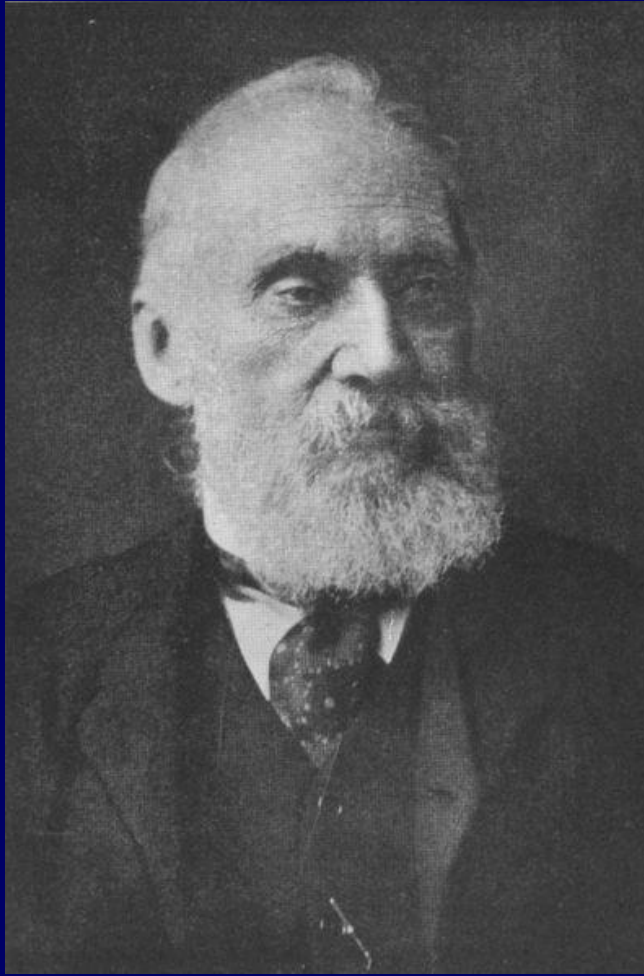
Solution

$$T = T_0 \operatorname{erf}\left(\frac{z}{2\sqrt{\kappa t}}\right)$$

William Thomson, Lord Kelvin (1824–1907)

# Lord Kelvin error

1862- age of the Earth is between 20 and 400 Mln yrs



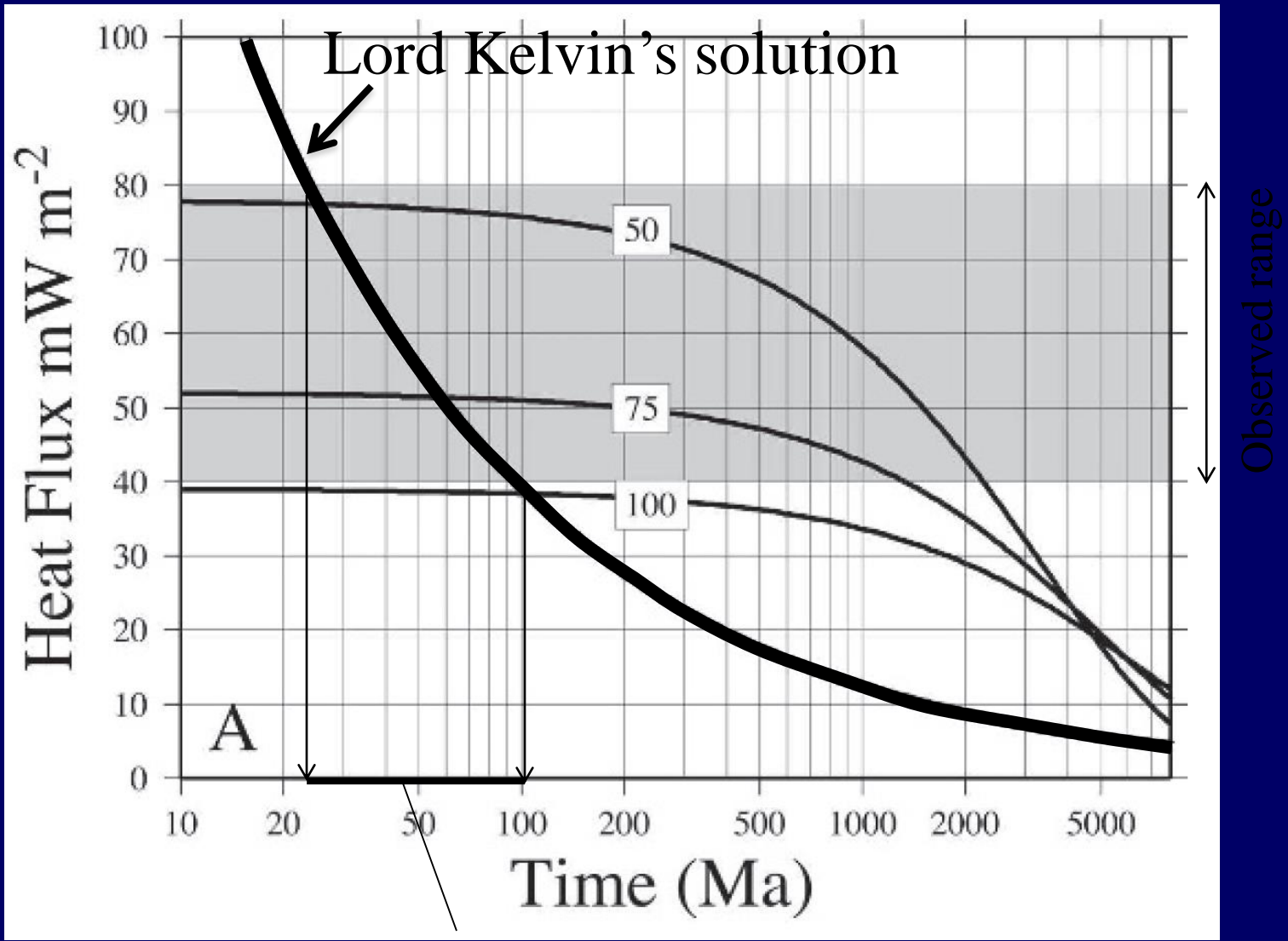
Solution

$$\frac{\partial T}{\partial z} \Big|_{z=0} = \frac{T_0}{\sqrt{\pi k t}}$$

$$t = \frac{1}{\pi k} \left( T_0 / \frac{\partial T}{\partial z} \Big|_{z=0} \right)^2$$

William Thomson, Lord Kelvin (1824–1907)

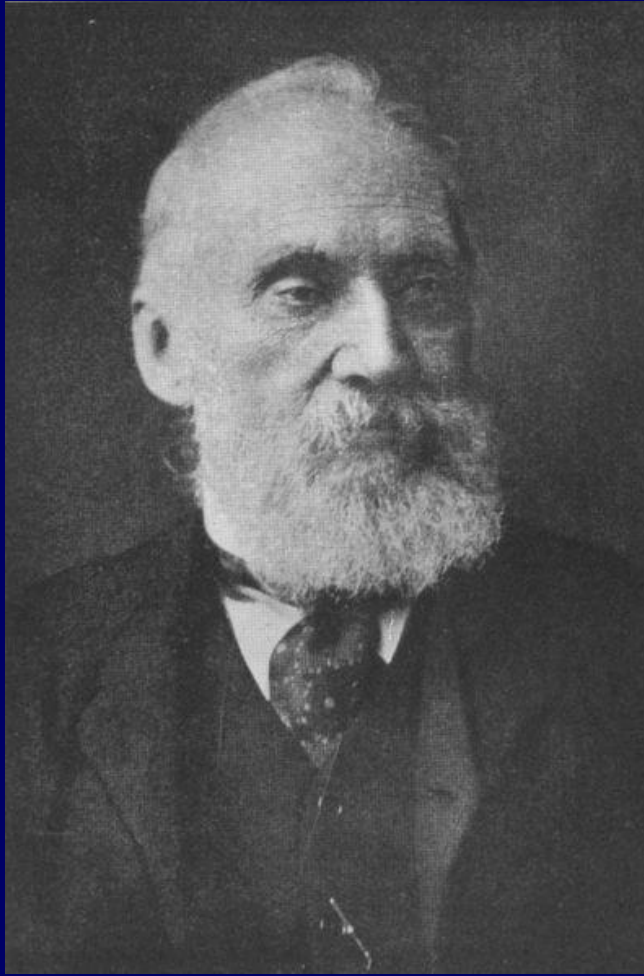




Age=25-100 Ma

# Lord Kelvin error

**1862- age of the Earth is between 20 and 400 Mln yrs**



Geologists were strongly against such short time, but could not find physical objections !

**William Thomson, Lord Kelvin (1824–1907)**

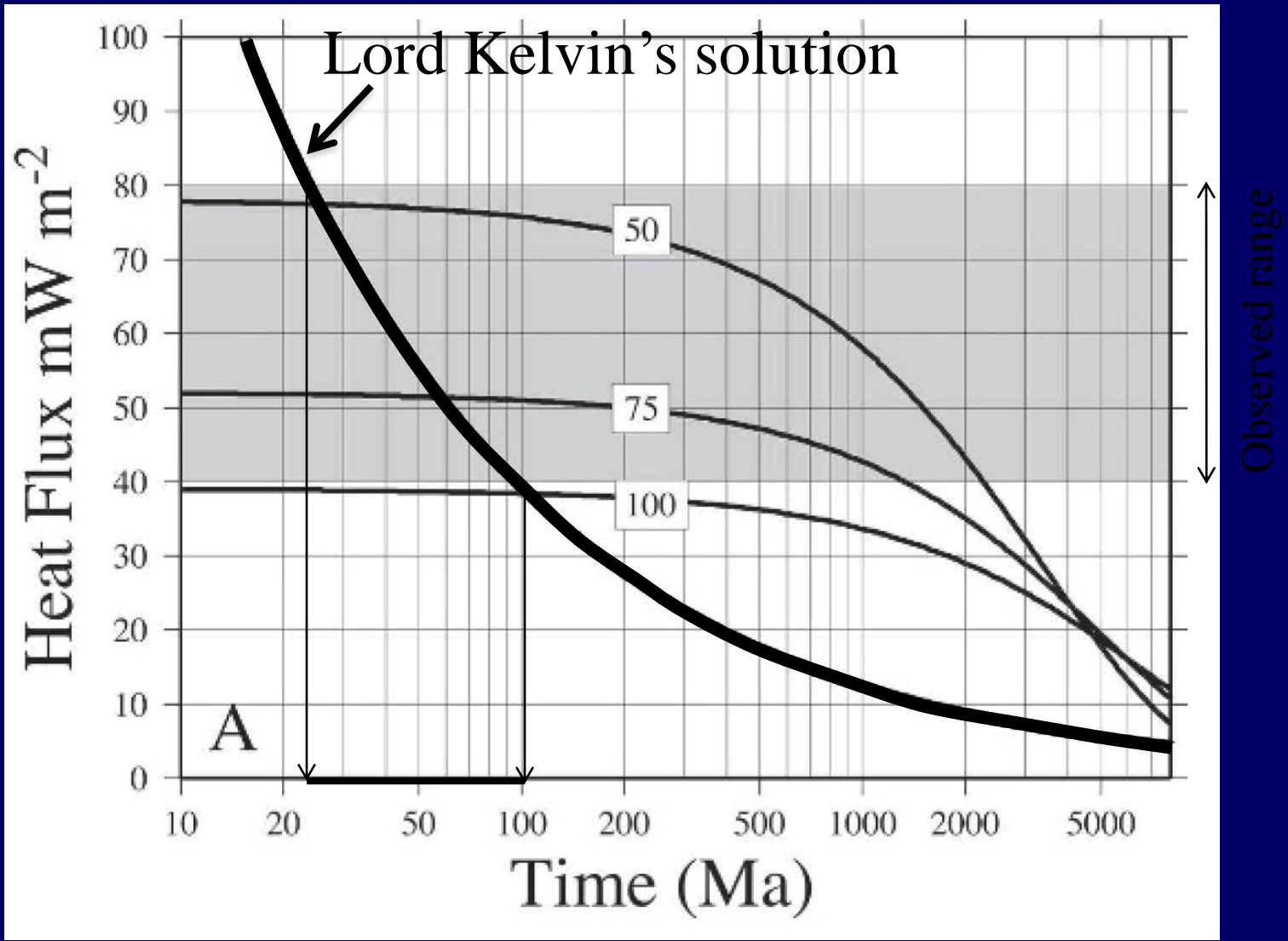
# Does consideration of radioactivity help?

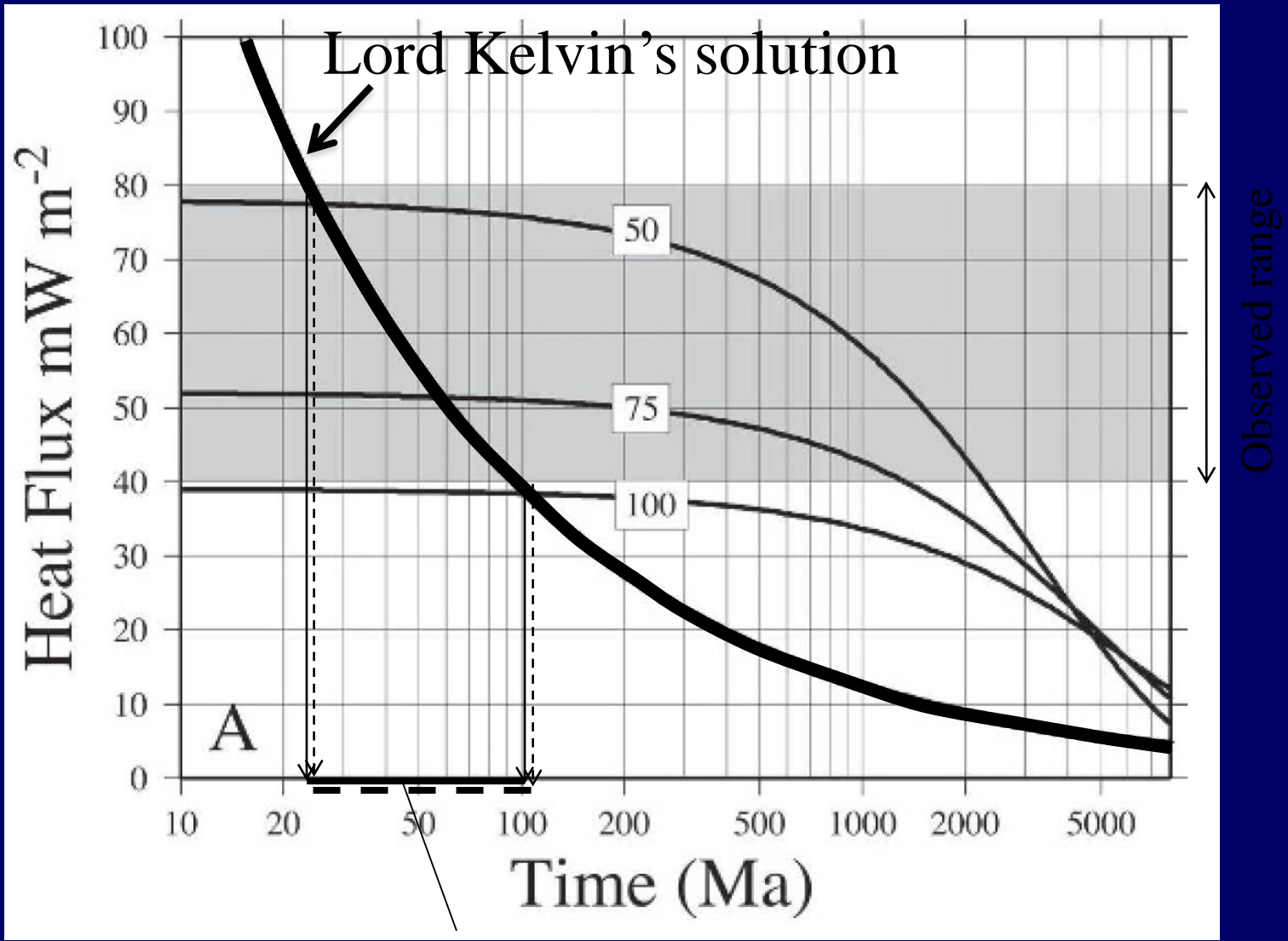
Entire radiogenic heat production for the Earth is about  $2 \times 10^{13}$  W

If distributed in the Earth homogeneously it gives volumetric heat production rate of  $A = 2 \times 10^{-5}$  mW/m<sup>3</sup>

Surface layer of thickness H will generate heat flow  $J = H \cdot A$ .

For  $H = 100$  km,  $J = 2$  mW/m<sup>2</sup>

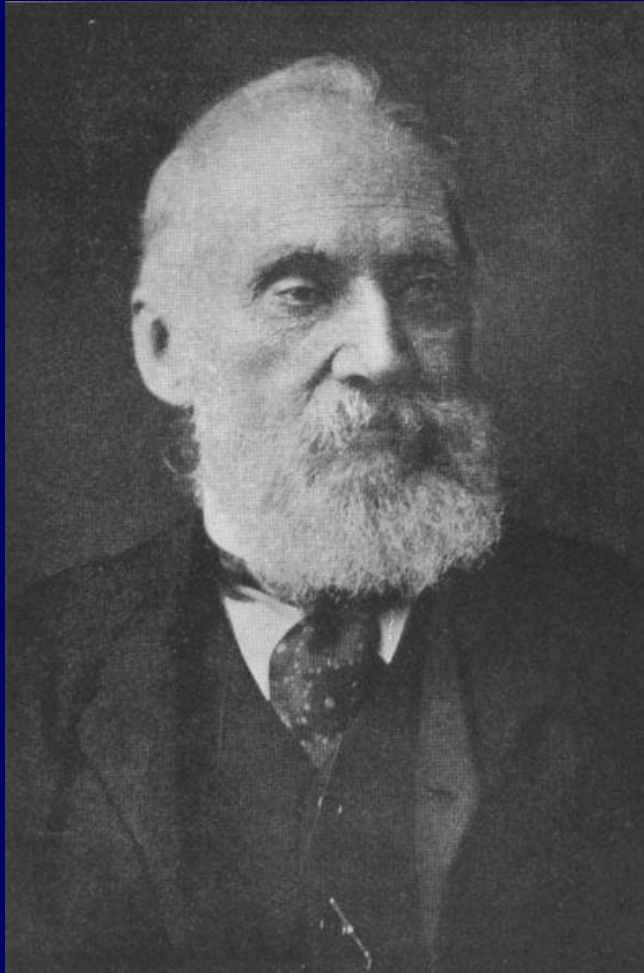




Correction is much too small!

# Lord Kelvin error

**1862- age of the Earth is about 20 Mln yrs**



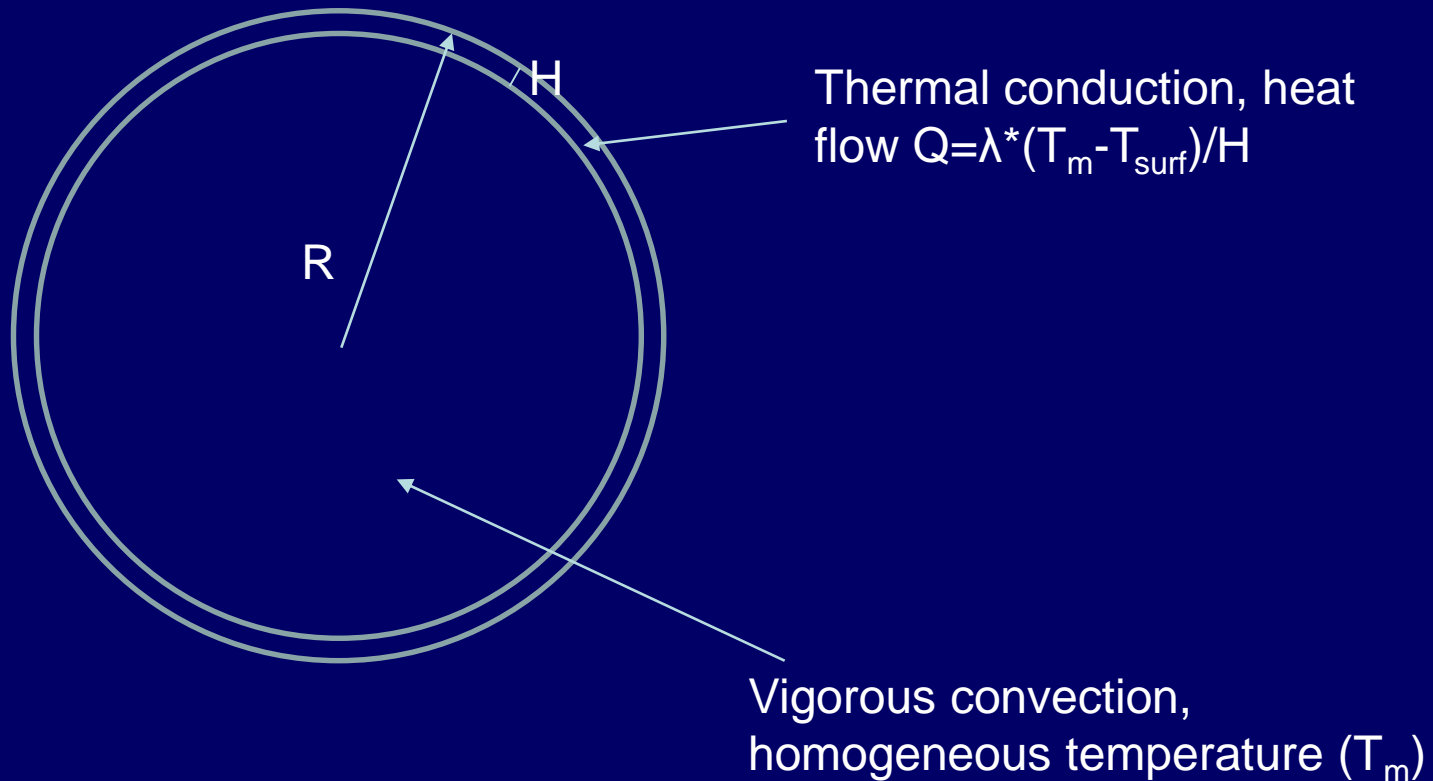
**1895- age of the Earth increases to few Bln. Yrs**



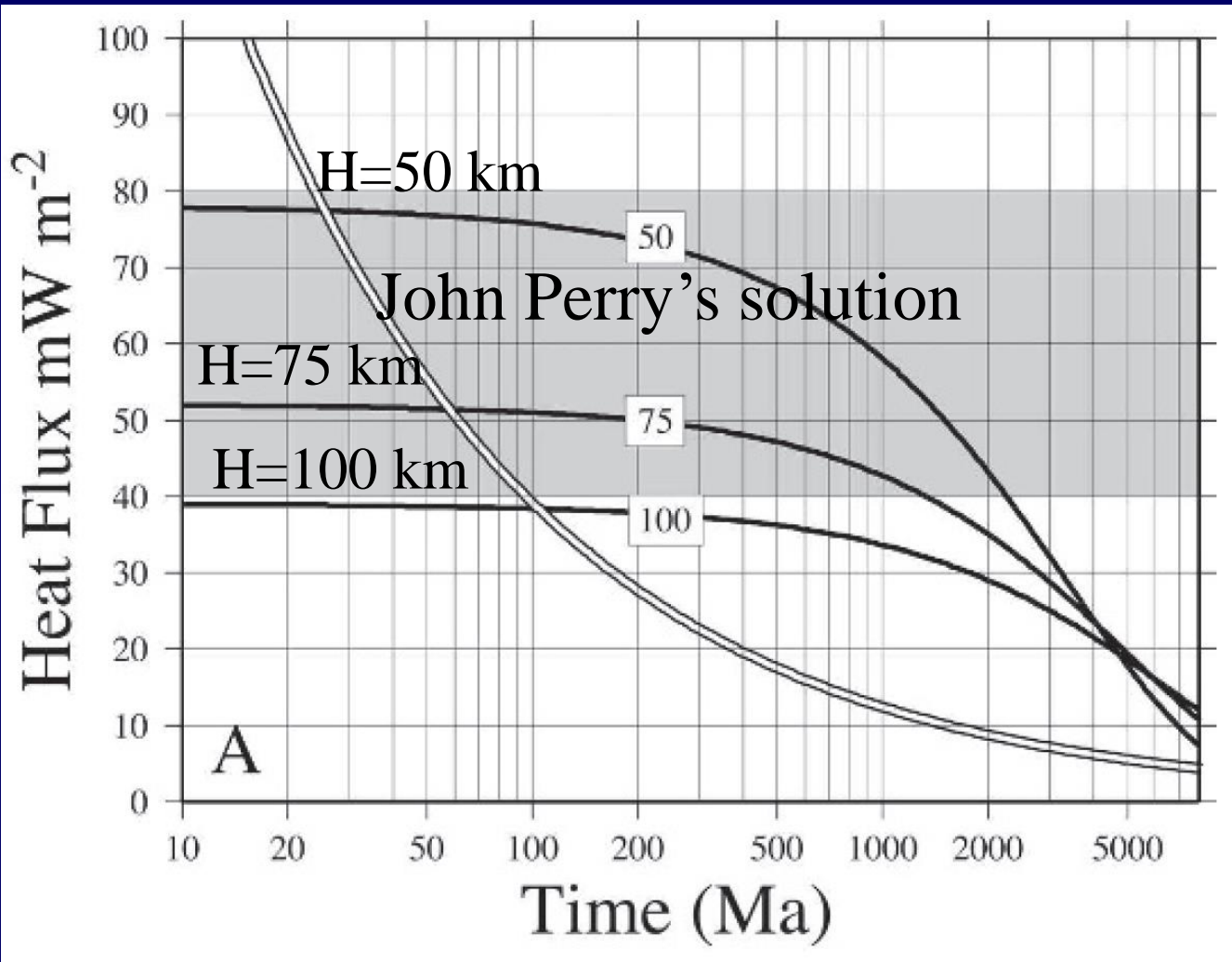
**William Thomson, Lord Kelvin (1824–1907)**

**John Perry (1850-1920)**

Perry assumed that inner part of the cooling Earth beneath the shell with thickness  $H$  was/is vigorously convecting. In this case heat from the deep Earth is efficiently transmitted to the surface

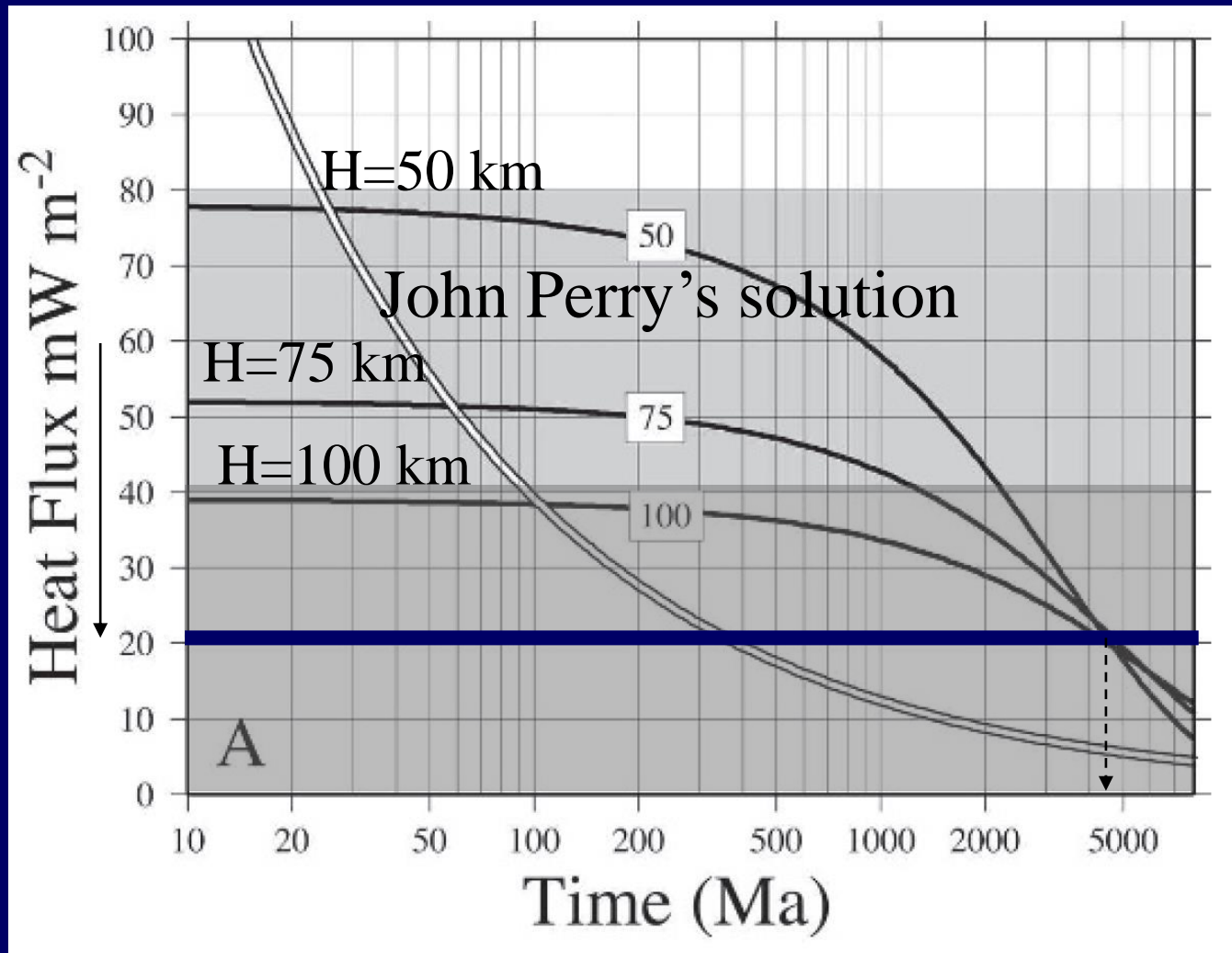


# Perry's solution





When we add radiogenic heat production of the entire Earth, that gives 40 mW/m<sup>2</sup> heat flux; then Perry's model must explain surface heat flux reduced by 40 mW/m<sup>2</sup>



## Lord Kelvin errors:

1. **Assumed conductive (slow) heat transfer in the entire Earth= ignored convection in the Earth (Major error)**
2. Did not consider radiogenic heat production (not known at that time)- less important error

If Lord Kelvin respected the intuition of geologists and supported John Perry, geophysicists would invent mantle convection already in year 1895!

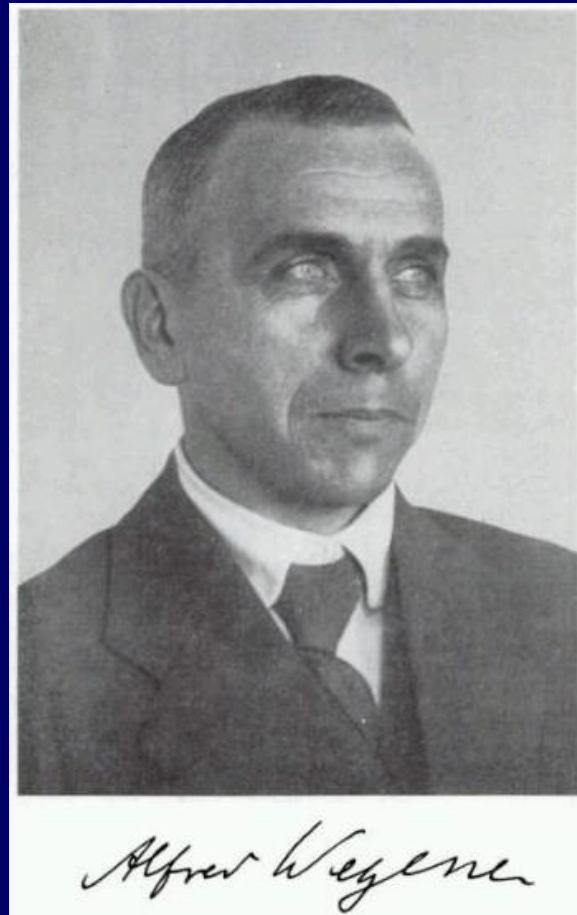
If Lord Kelvin respected the intuition of geologists and supported John Perry, geophysicists would invent mantle convection already in year 1895!

That would bring closer and make much easier establishment of the Earth-Science main theory—Plate Tectonics and Alfred Wegener's idea would be much better recognized during his life!

# From Continental Drift to Plate Tectonics

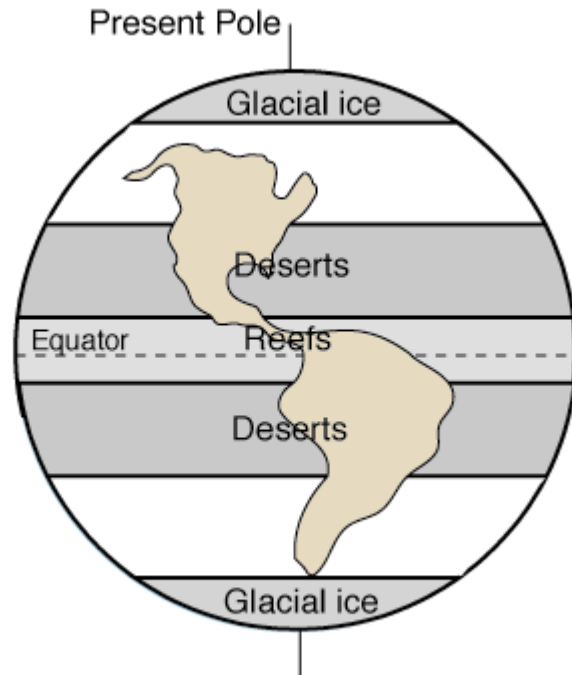
1915 first edition of book

*“Die Entstehung der Kontinente und Ozeane”*



**Alfred Lothar Wegener (1880 –1930)**

# Paleoclimate argument



Present-day climate zones and associated geologic features define a pattern relative to the pole of rotation.

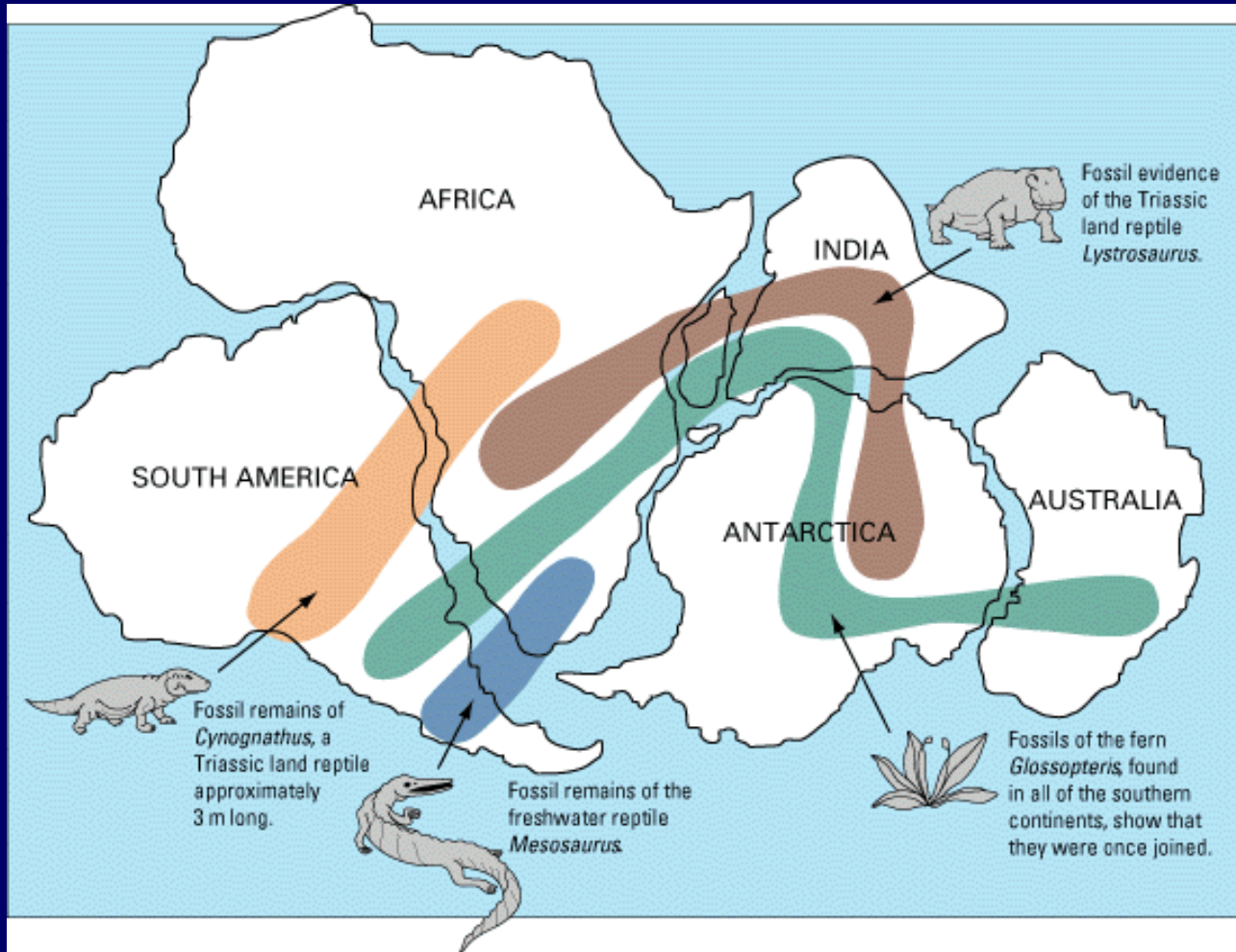


Grooves carved by glaciers (shown by arrows) provided evidence for continental drift. This diagram assumes the continents were in their present-day locations.



The distribution of glacial features can be best explained if the continents were part of Pangaea.

# Fossils distribution argument



Wegener suggested that continents moved by thousands of km based on large range of various observations: very valuable approach in geodynamics

The next step should be recognition of reasons, i.e. origin of forces required to move the continents



Wegener suggested rotational and tidal forces as a possible driver

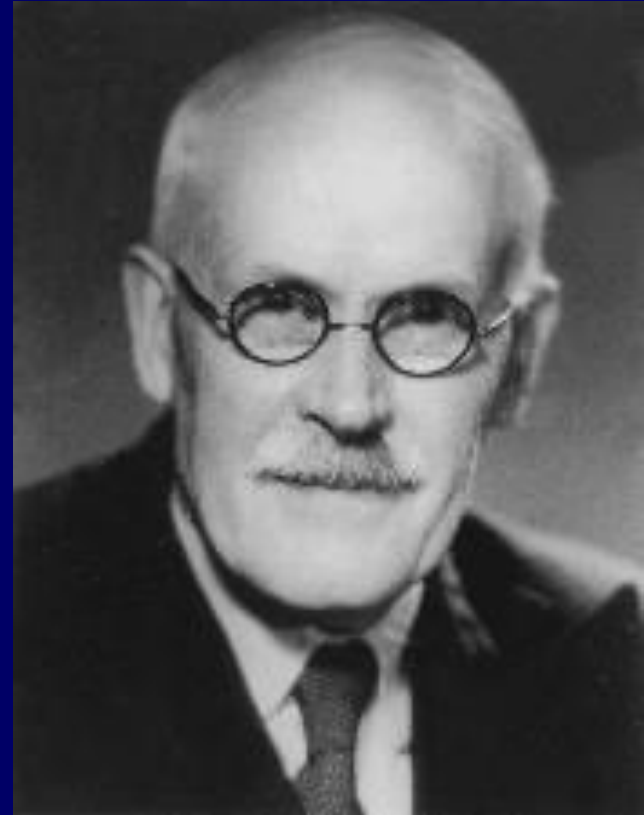
It was soon recognized that rotational and tidal forces are insufficient

# From Continental Drift to Plate Tectonics

## 1912- Continental Drift hypothesis



**Alfred Lothar Wegener (1880 –1930)**



**Sir Harold Jeffreys (1891 – 1989)**

Fatal argument against continental drift :

*most of the crust and mantle is solid and elastic (elastic shear waves pass through),*  
**hence continents can not drift by**  
**1000 km**

Contra-argument:

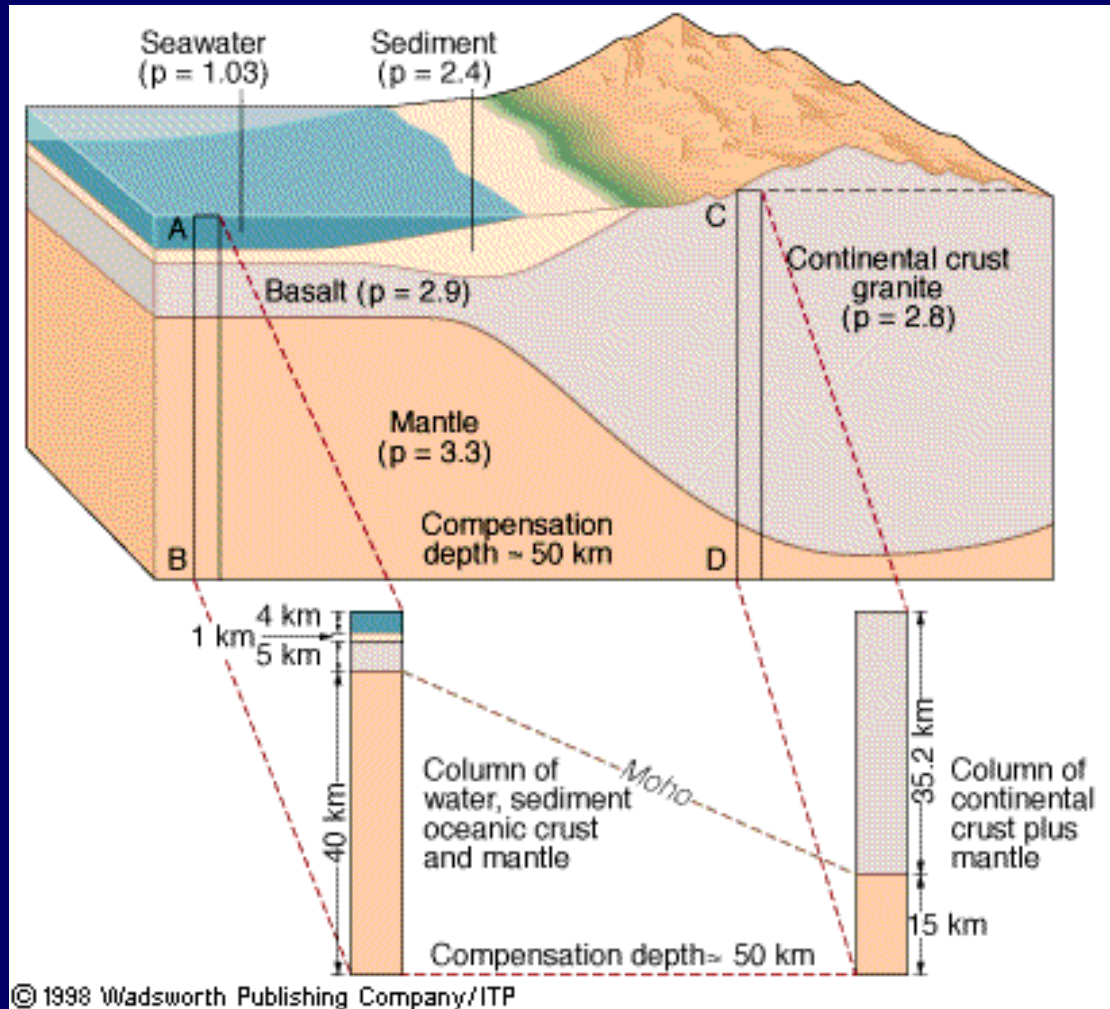
*solid-flow is possible at geological time scale - ductile rheology*

# Isostasy was already known since 1885!

*isostasy:*

columns of mass must be the same at a certain depth (compensation depth) ~ 50 km

continents have roots and stick-up

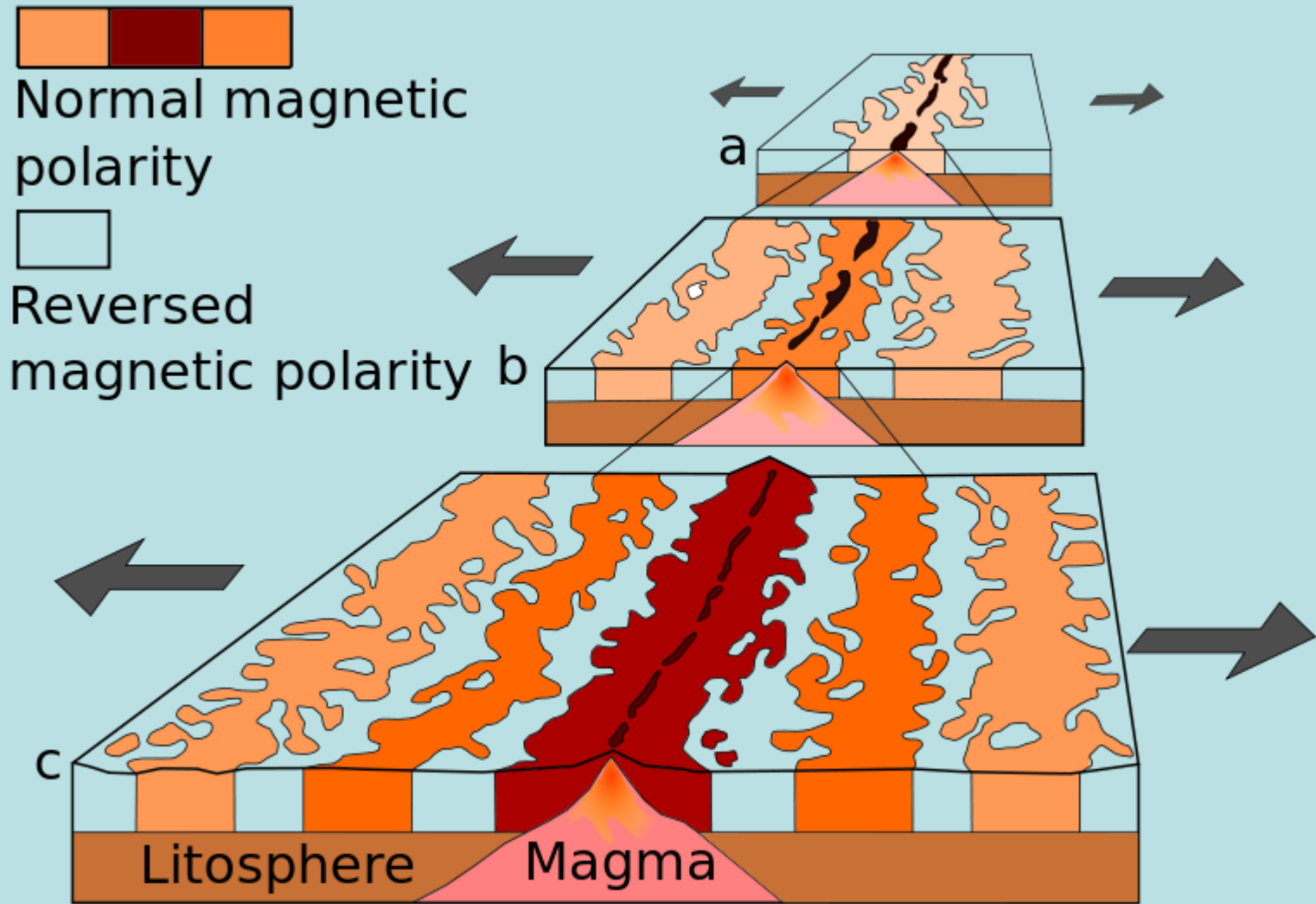


# 1928- Mantle convection as a driver of continental drift



**Arthur Holmes (1891 – 1989)**

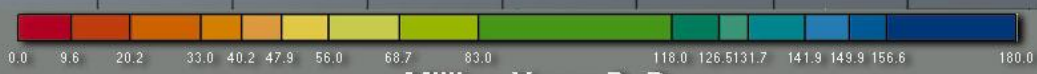
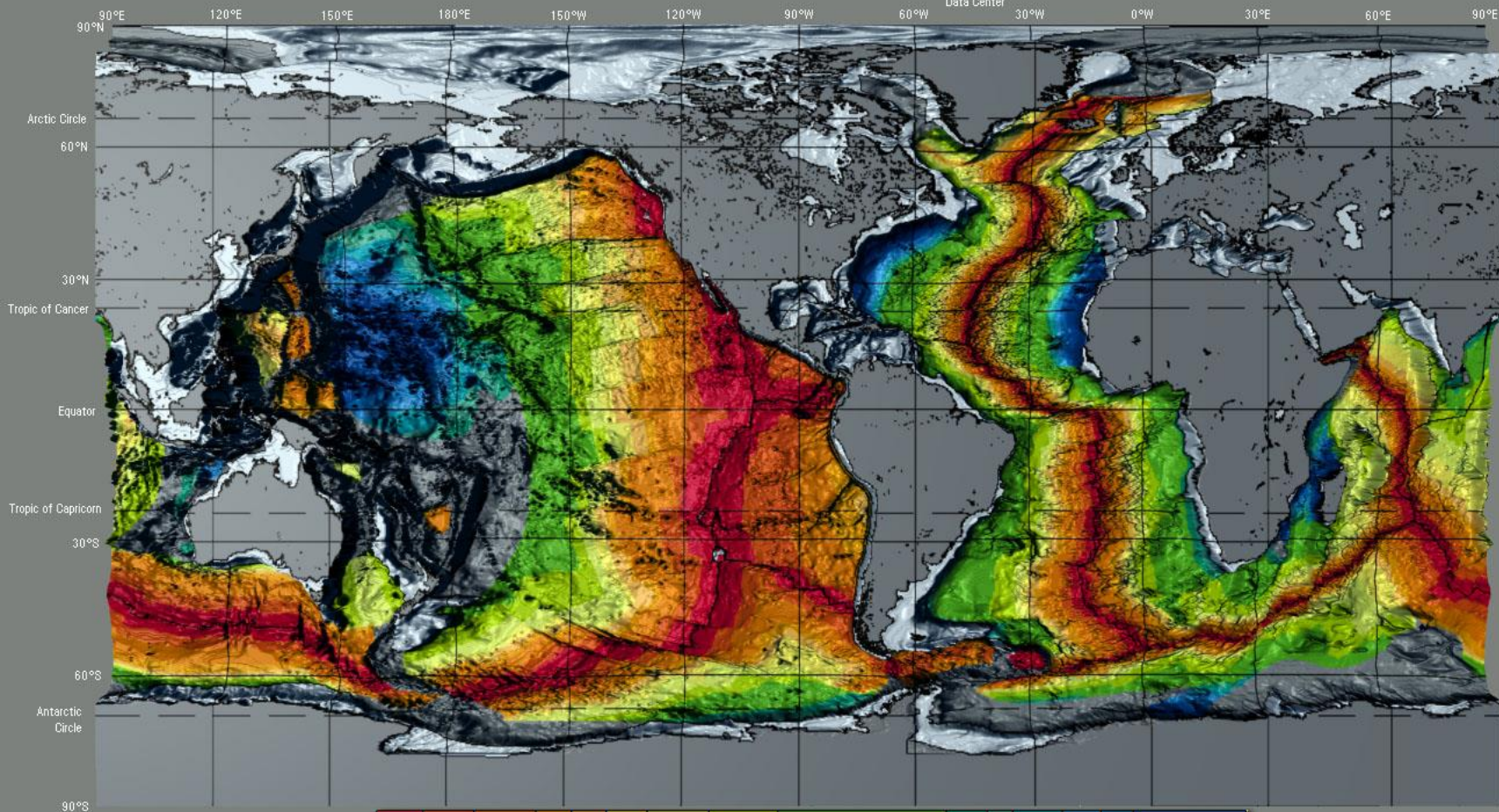
# Great 1960s!



# Crustal Age



National Geophysical  
Data Center

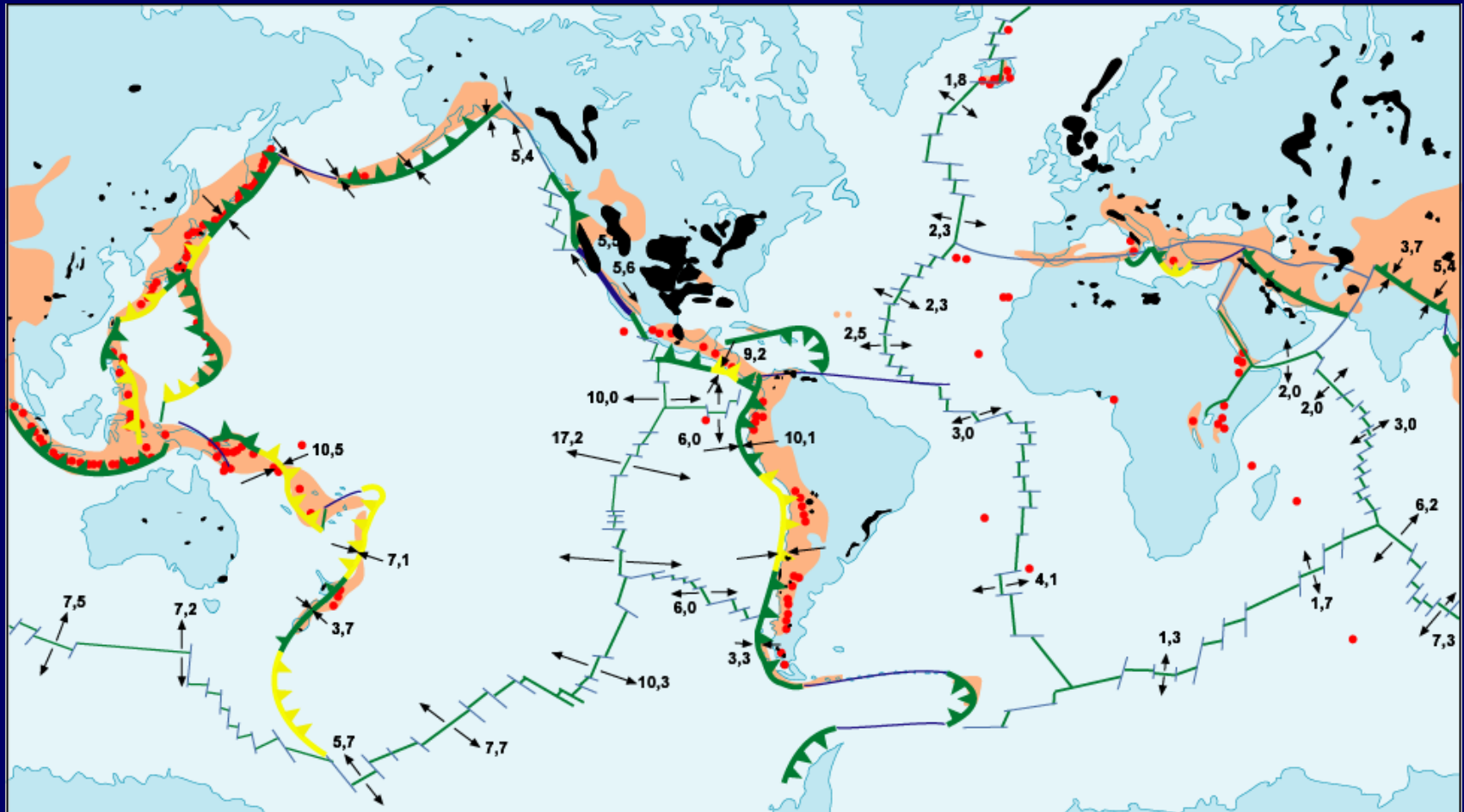


Million Years B. P.

Data for the image from "Digital Age Map of the Ocean Floor" by Müller, Roest, Royer, Gahagan, and Schlater, Scripps Institution of Oceanography Ref. Series No. 93-30

For information on this and other images produced by NGDC's Marine Geology and Geophysics Division, contact Peter Sloss at [psloss@ngdc.noaa.gov](mailto:psloss@ngdc.noaa.gov)

# Plates



## convergent plate margins

erosive accretionary transform

## divergent plate margins

← → 7,7 spreading rate (cm/a)

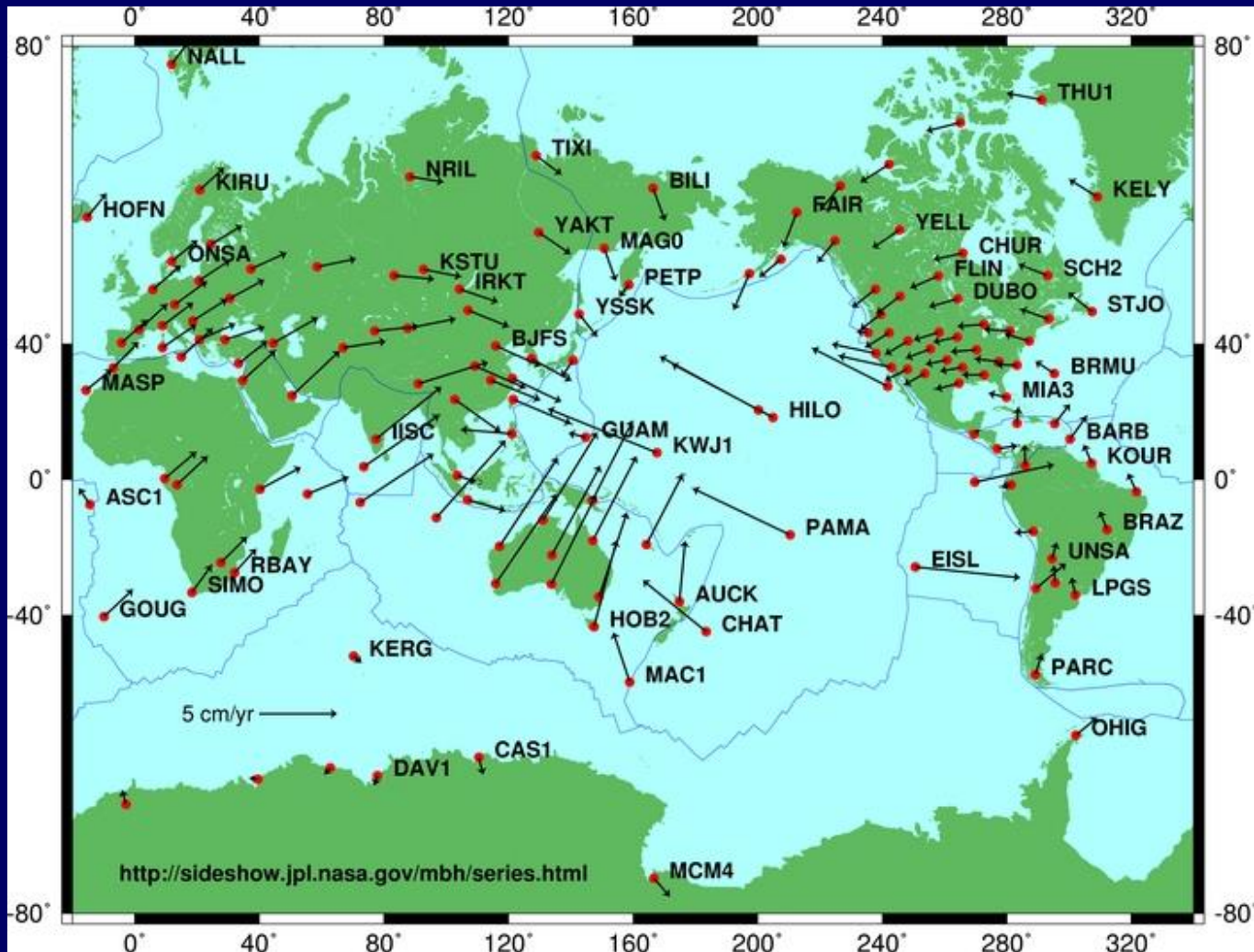
earthquake zones

active volcanoes

hydrocarbons

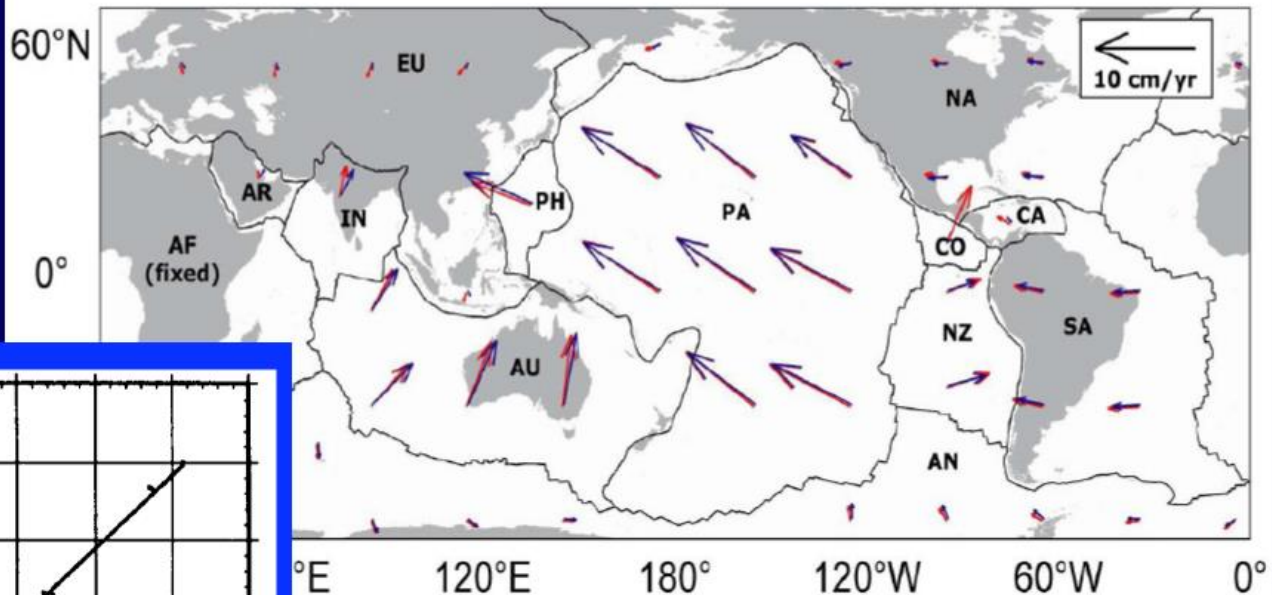


# GPS-revolution



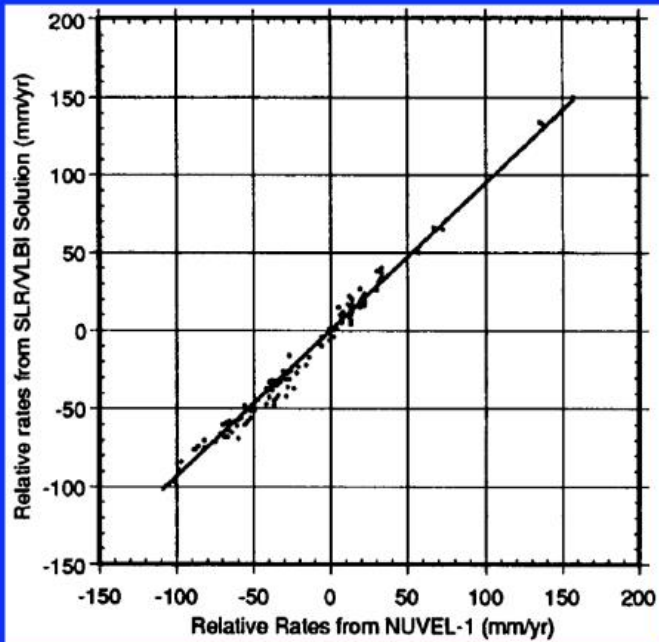
# GPS revolution

Comparison of recent (3.2 m.y.) and present-day plate motions



(3.2 m.y. ago)

present day)



3 Myr average plate motion model

Plate tectonics model is verified !

# What causes plate tectonics?

Google search top:

How Do Plates Move?

Plates at our planet's surface move because of the intense heat in the Earth's core that causes molten rock in the mantle layer to move. It moves in a pattern called a convection cell...

**Source:**

[http://www.windows2universe.org/earth/interior/how\\_plates\\_move.html](http://www.windows2universe.org/earth/interior/how_plates_move.html)

# What causes plate tectonics?

Google search top:

- **Q:**What causes tectonic plates to move?
- **A:QUICK ANSWER**
- The three primary causes for tectonic plate movement are the convection of material in the mantle, gravity and the rotation of the planet.

**Source:**

<https://www.reference.com/science/causes-tectonic-plates-move-974f091e6fc56047>

Is convection in the mantle sufficient to produce plate tectonics?

What kind of tectonics  
should be expected with  
“normal” mantle convection?

$$\eta \approx \exp(H_a / nRT)$$

Stagnant-lid tectonics →  
convection beneath the outer  
shell (lid) and no much  
deformation near the surface

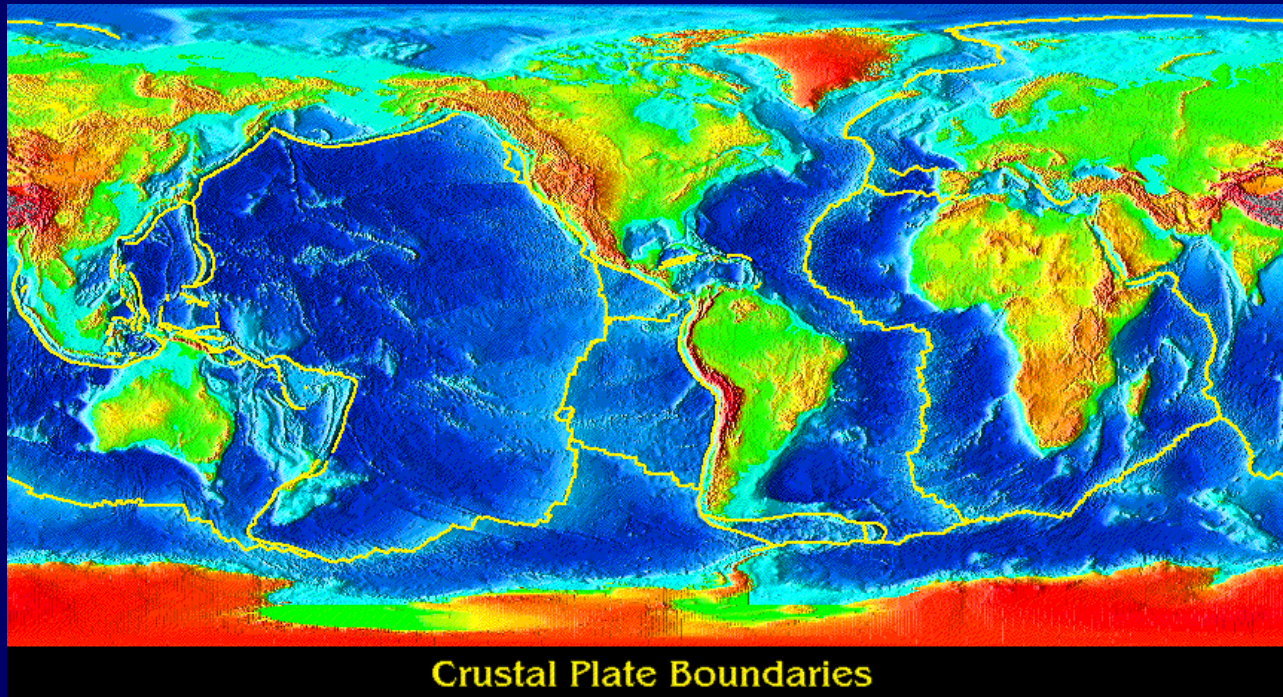
**NOT Plate Tectonics!**

Surface would not move by  
1000 km.

Additional ingredient is required.

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Surface would not move by  
1000 km.

Additional ingredient is required.



**Weak plate boundaries**



# Key factors for plate tectonics

1. Mantle convection
2. Weak plate boundaries, and particularly, weak interfaces of subducting slabs making subduction interfaces the weakest faults

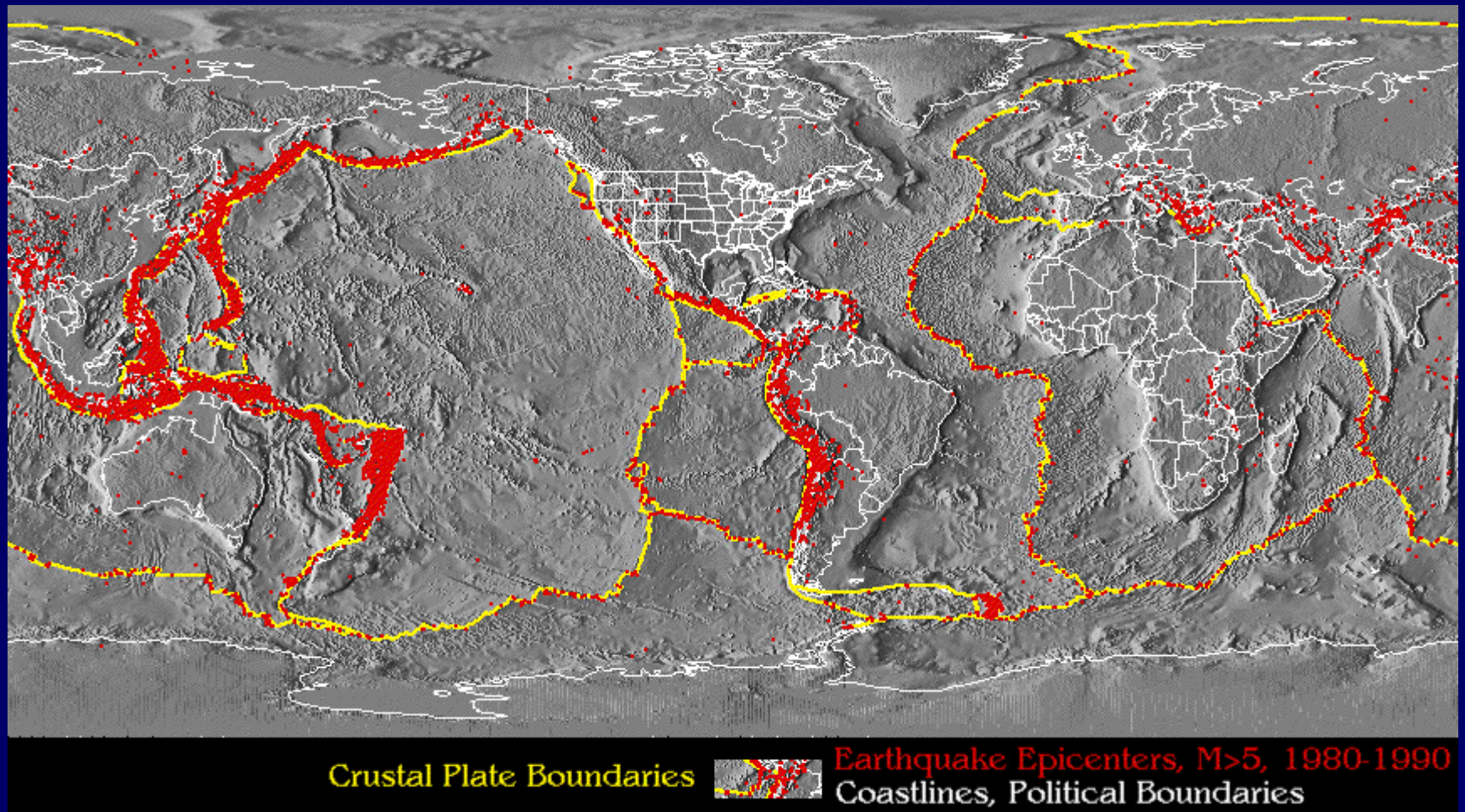
**Is “weakness” of plate boundaries consistent with appearance there greatest earthquakes?**

# Plate tectonics and great earthquakes

At geological-time scale (10-1000 Mln.y) signatures of Plate Tectonics are 1000 km -scale plate motions, large deformations at plate boundaries like mountain belts, rift zones and transform faults or Wilson Cycle

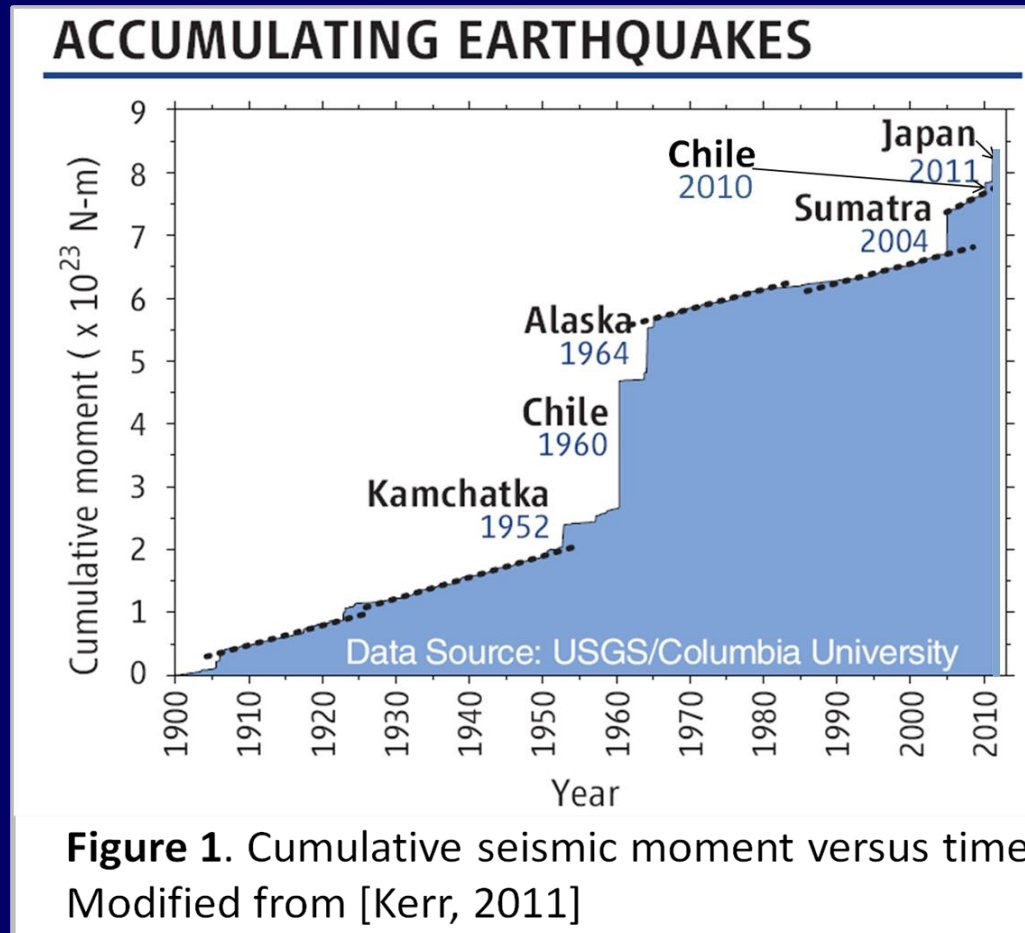
At time-scale of less than 1000 years signatures of Plate Tectonics are earthquakes at plate boundaries

# Earthquakes and plate tectonics



The greatest earthquakes occur in subduction zones

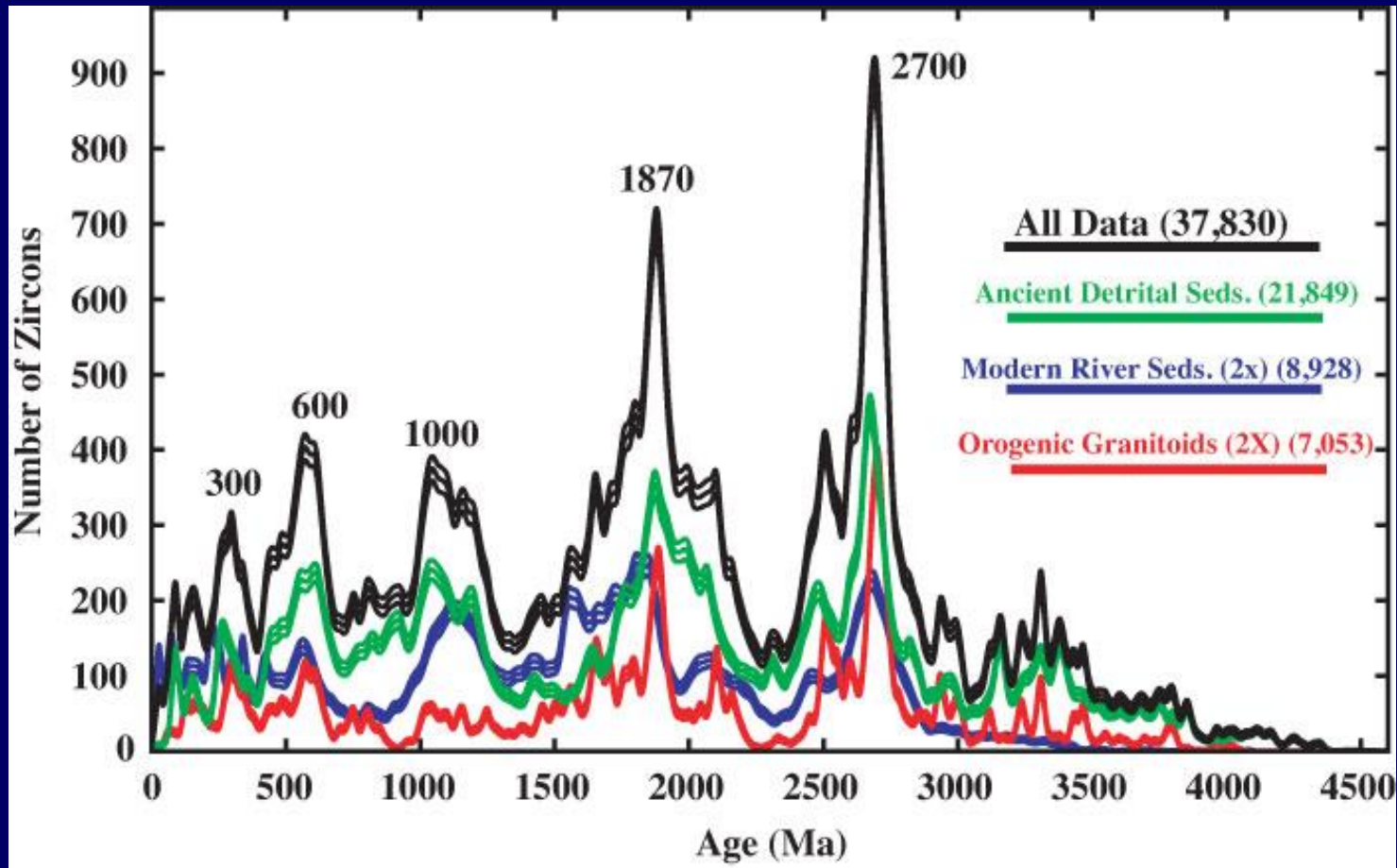
# Great Earthquakes challenges



Why the greatest earthquakes occur in the weakest zones? Do they indeed cluster?

# How and when the plate tectonics started at Earth?

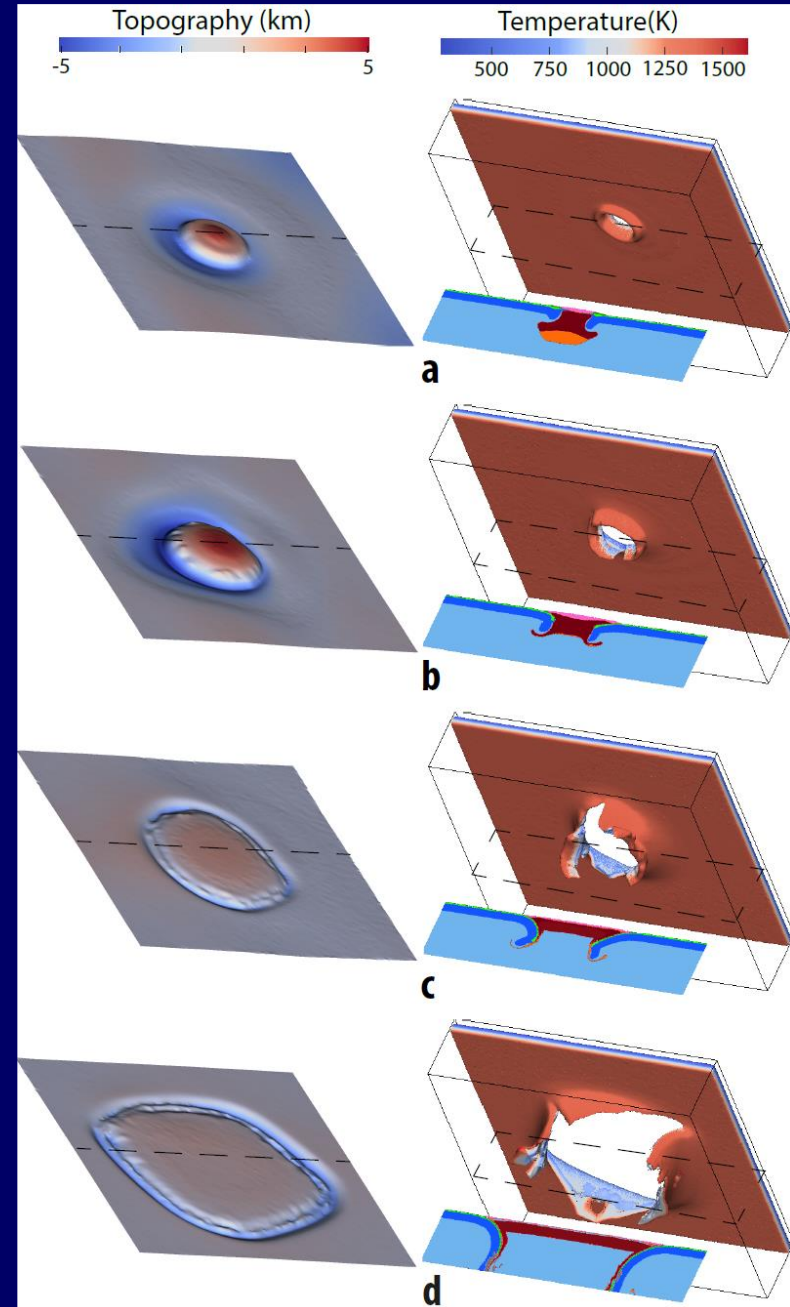
Zircon Age Distribution through time. Monitor of Continental Crust growth



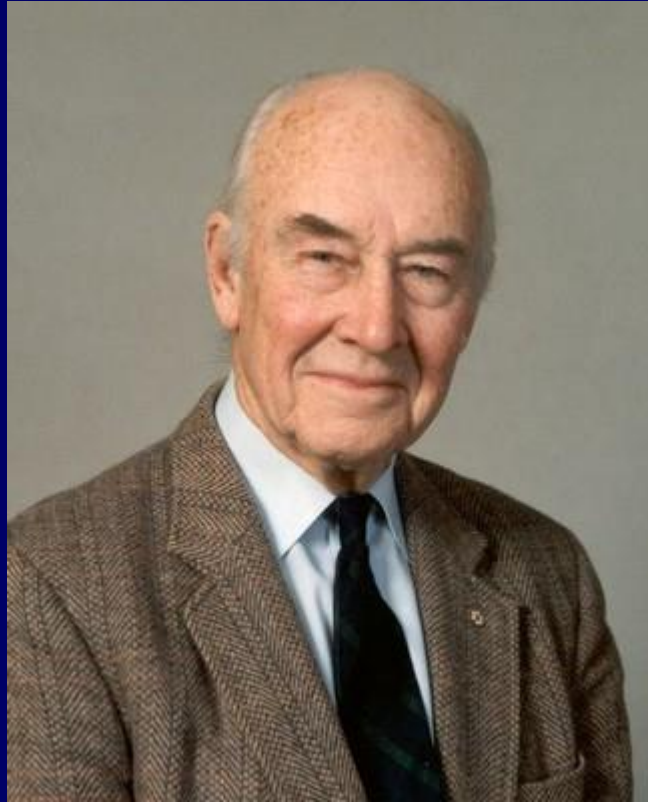
Condie & Aster, 2009

# How and when the plate tectonics started at Earth?

Brand-new 3D model for initiation of plate tectonics by mantle plume



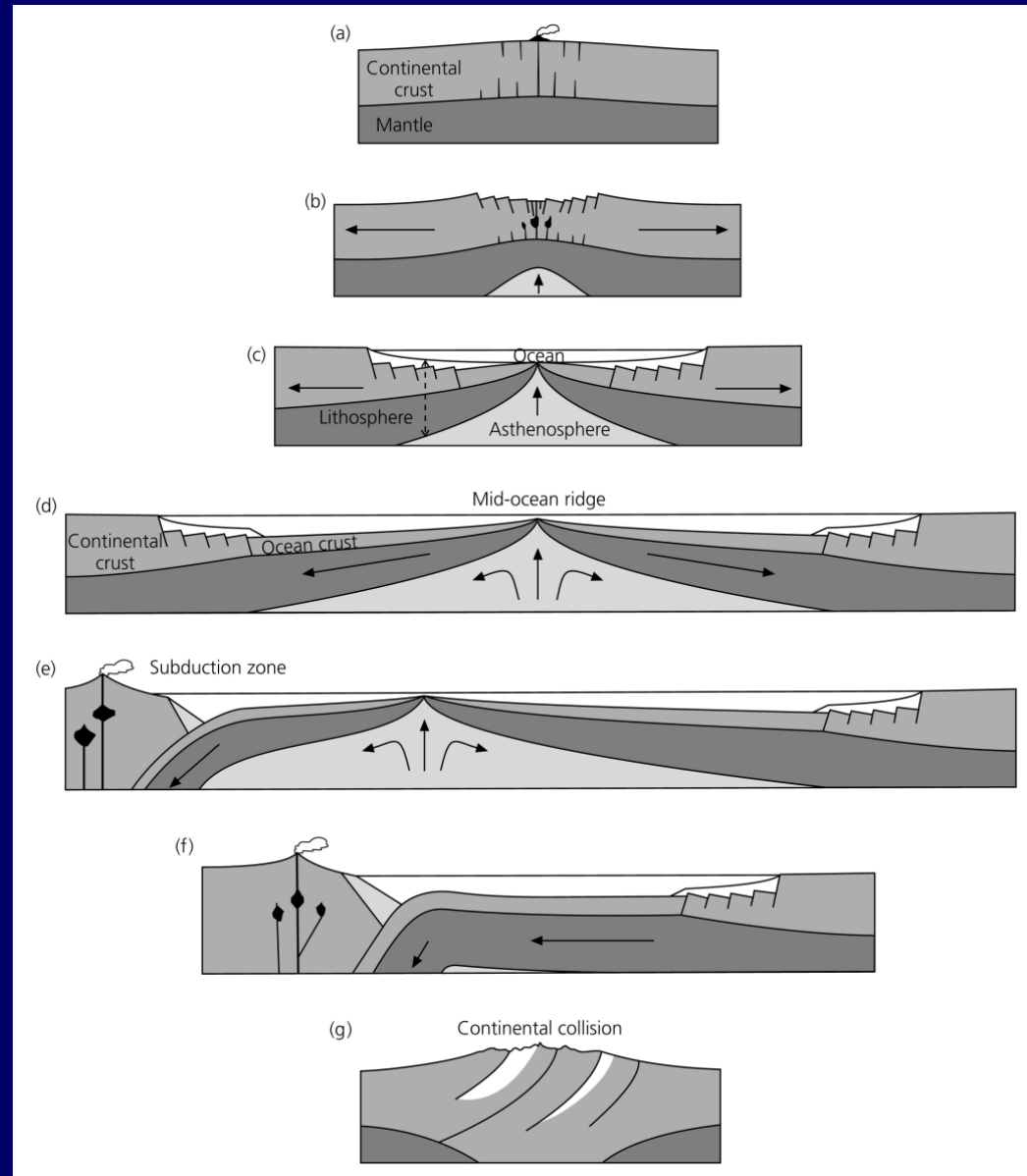
# Mysteries of Wilson cycle



John Tuzo Wilson (1908–1993)

# Wilson cycle

Physically difficult



No known examples

Physically very difficult



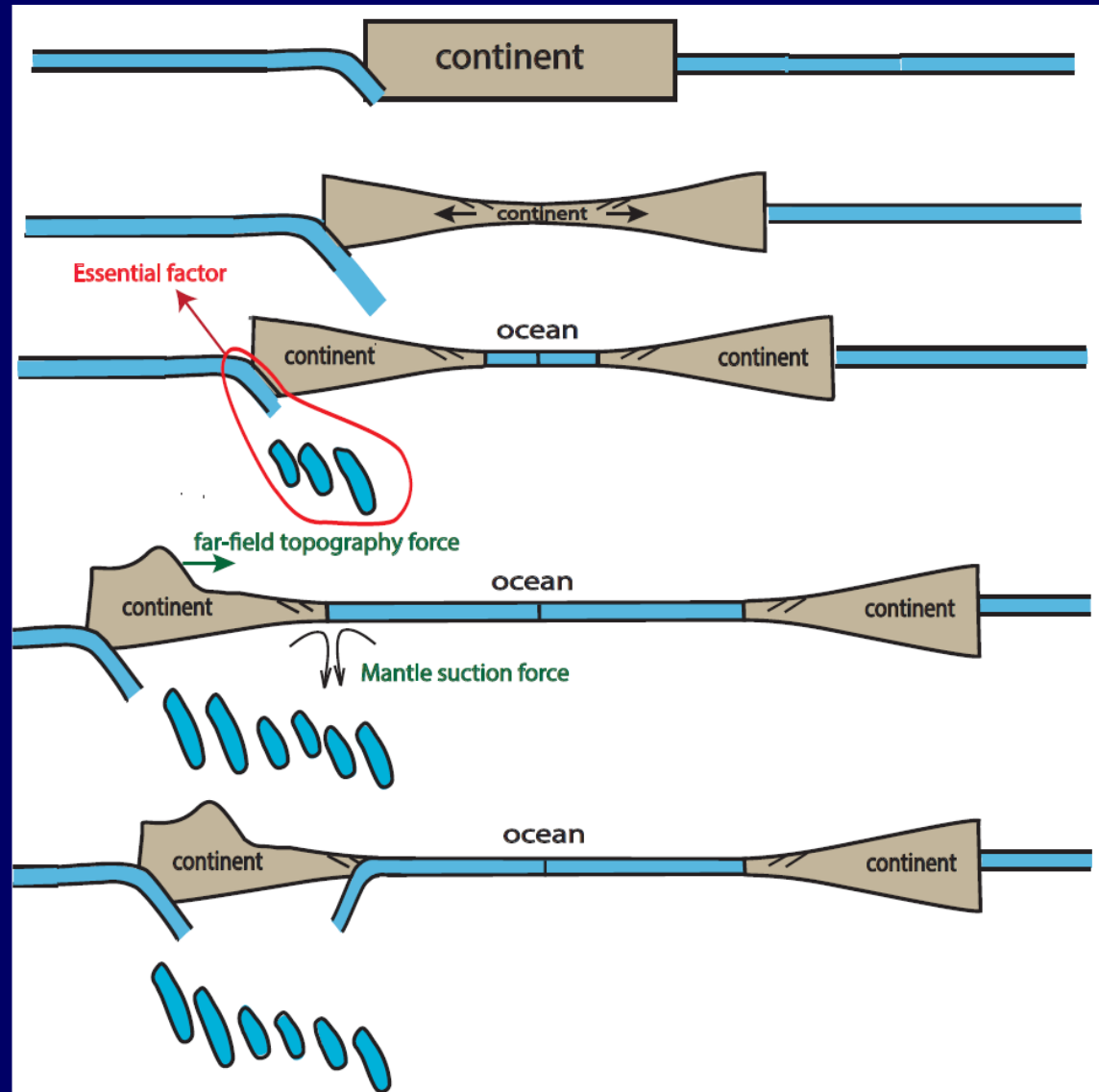
# Wilson Cycle challenges

How do the continents break up?

How do passive margins convert  
into active (subduction) margins?

# How do passive margins convert into active (subduction) margins?

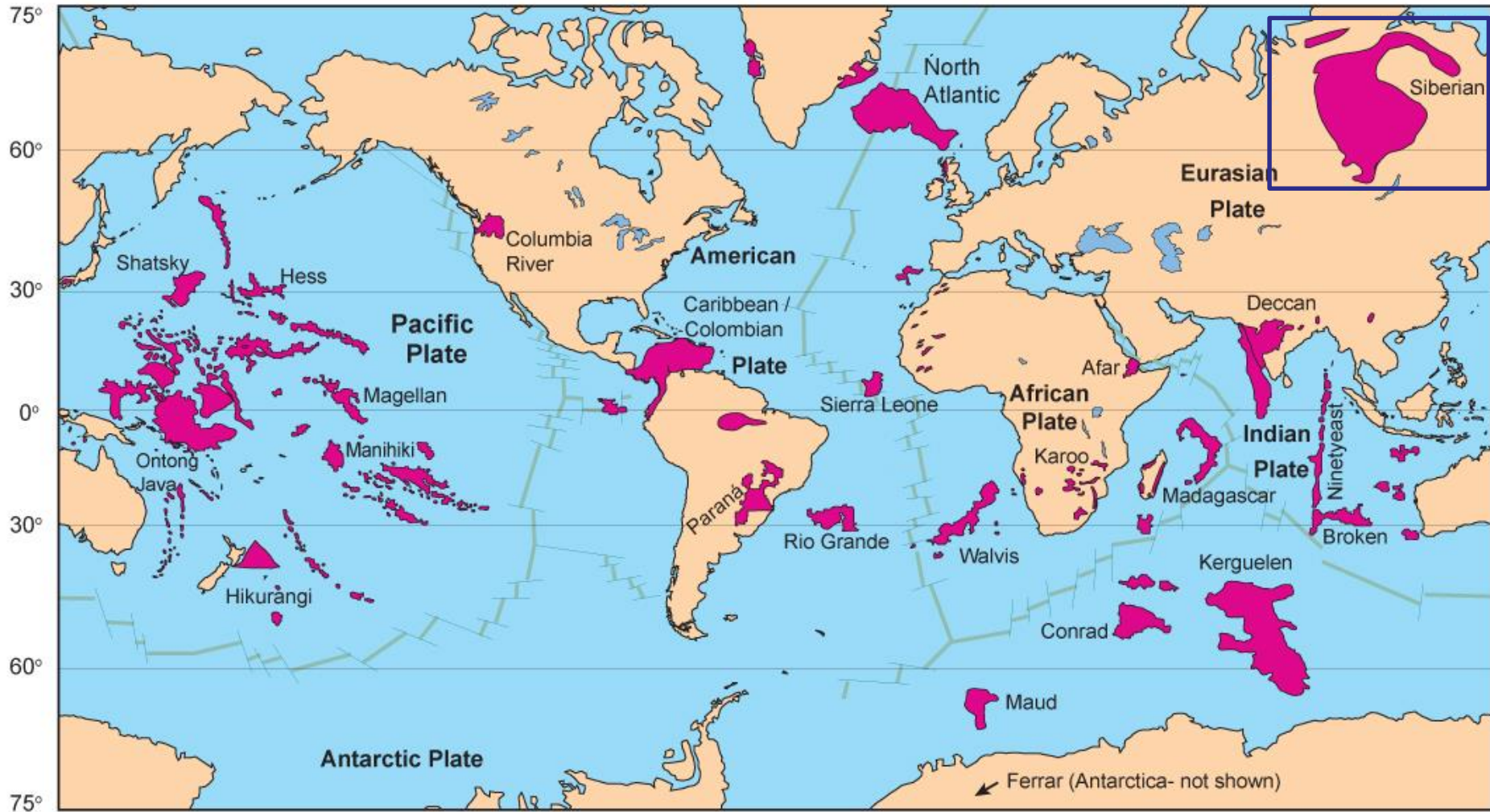
Brand-new model for initiation of subduction at passive margins



**In our course we will see ideas and models attempting to resolve these and other key problems of plate tectonics**

# Beyond the plate tectonics

# Large Igneous Provinces (LIPs)



After Saunders et al. (1992)

# Siberian LIP

- Over 4 mln. km<sup>3</sup> of magmas produced in less than 1 ma

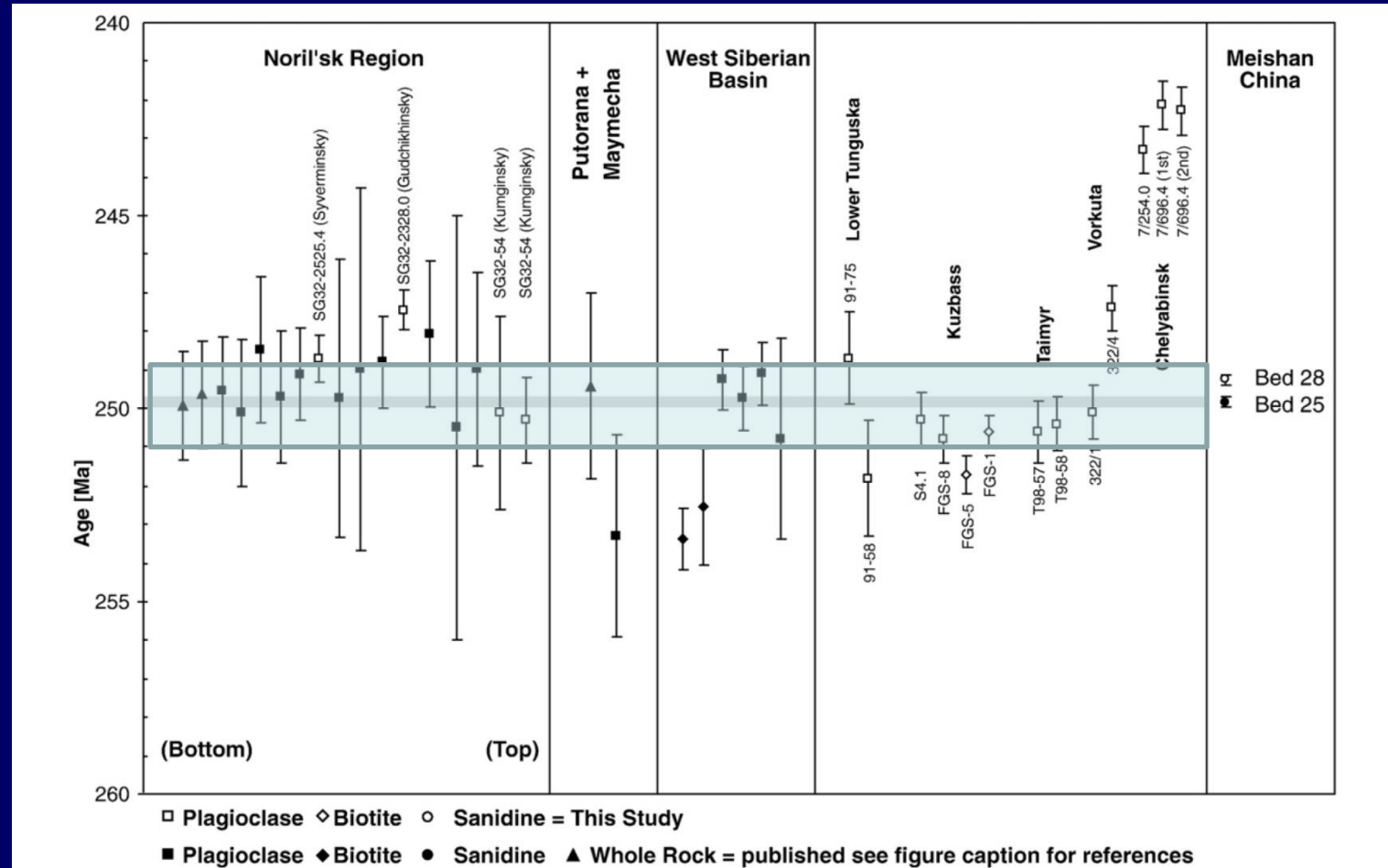
# Siberian LIP



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# Ar-Ar age of Siberian Flood Basalts

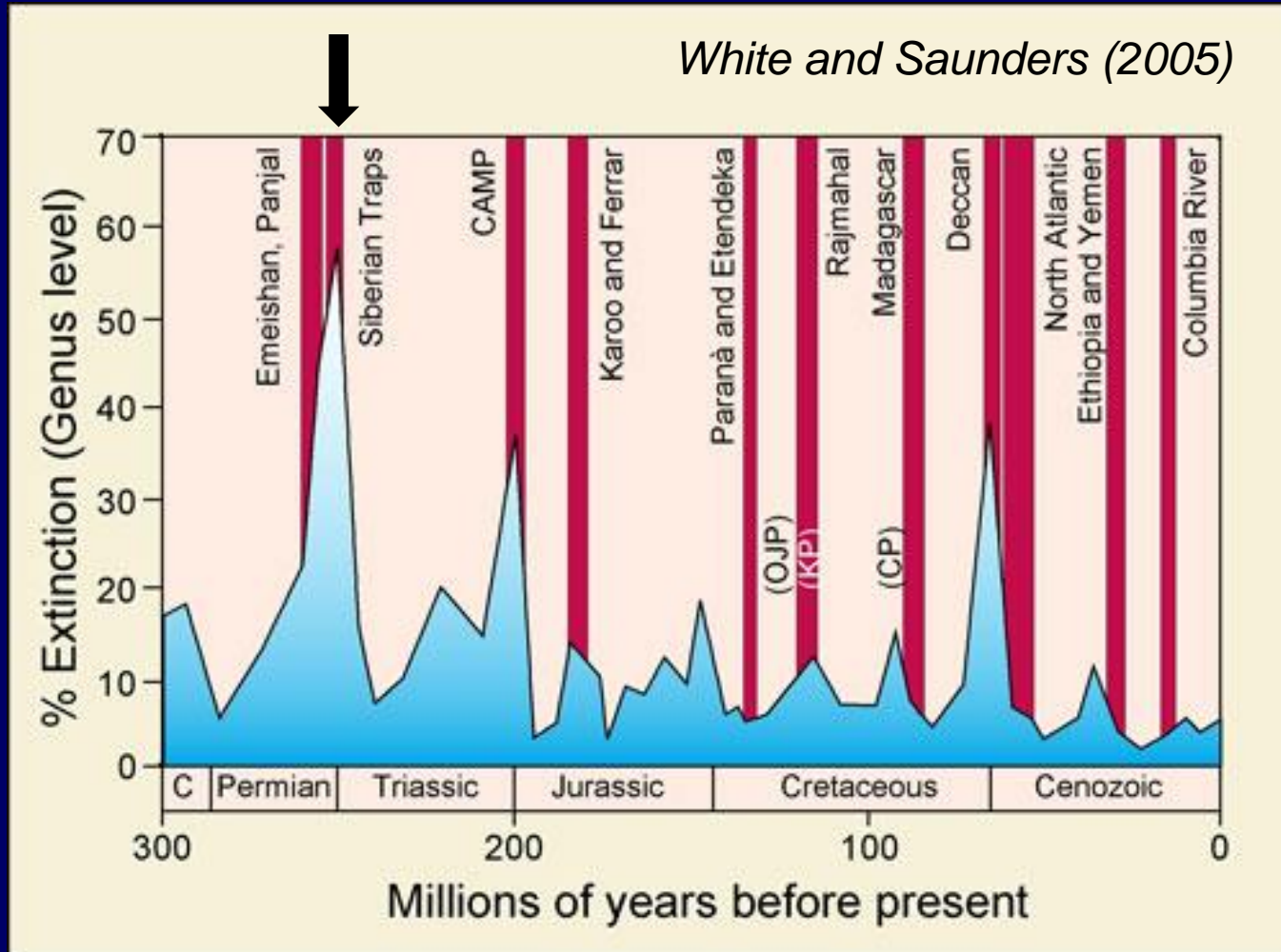
## $250 \pm 1.1$ Ma



Reichow et al, 2009



# LIPs correlate with mass extinction events

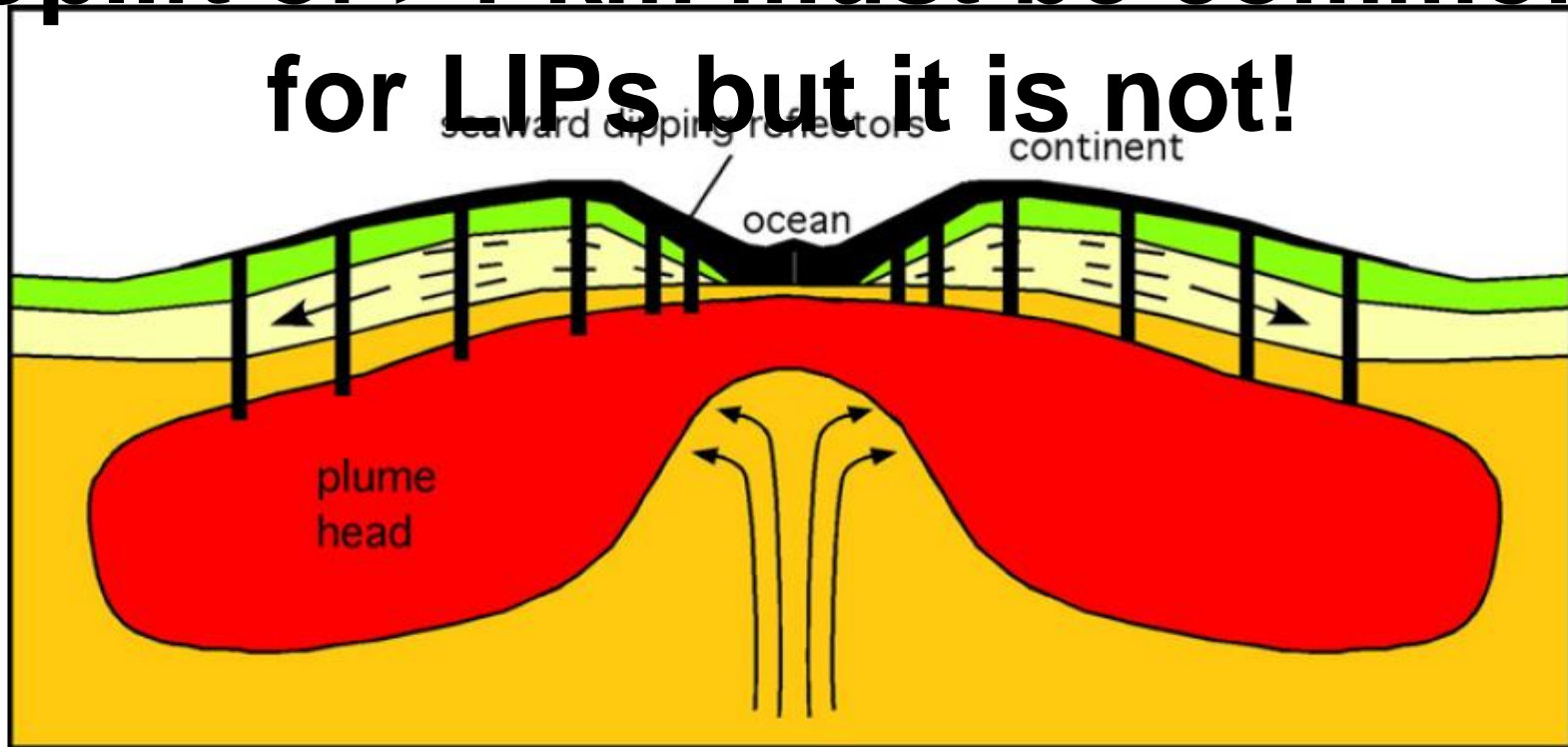


# Plume head model of LIPs

White and McKenzie, 1989; Richards et al., 1989,  
Campbell and Griffiths, 1990

*I.H. Campbell / Chemical Geology 241 (2007) 153–176*

**Uplift of  $>1$  km must be common  
for LIPs but it is not!**



How do LIPs form and how do they relate to plumes and plate tectonics?

Why in some cases LIPs are associated with mass extinctions and in other not?

**In our course we will see ideas and  
models attempting to solve key  
problems of LIPs**

# Equations

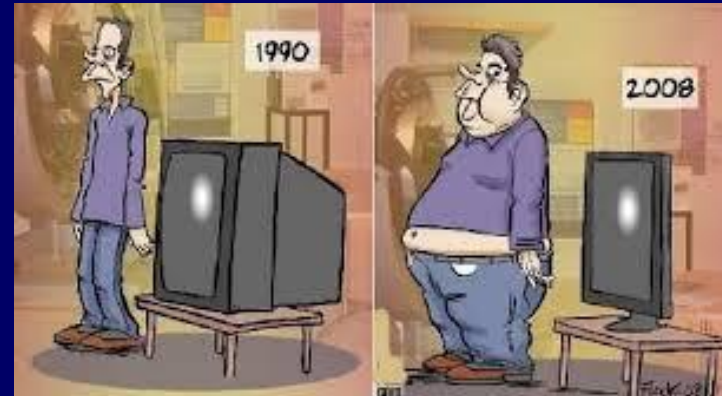
# Geodynamic modelling

## *Basic conservation laws*

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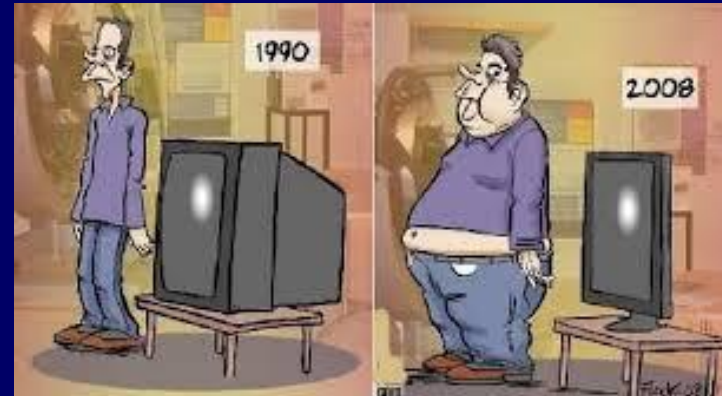
Mass conservation law:



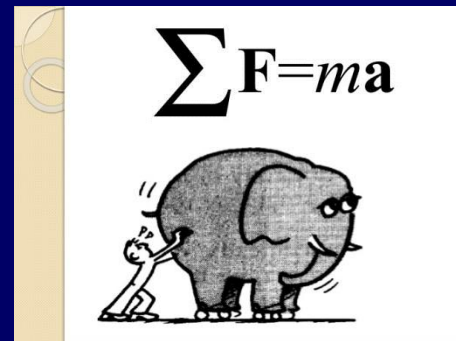
# Geodynamic modelling

## *Basic conservation laws*

Mass conservation law:



Momentum conservation law:

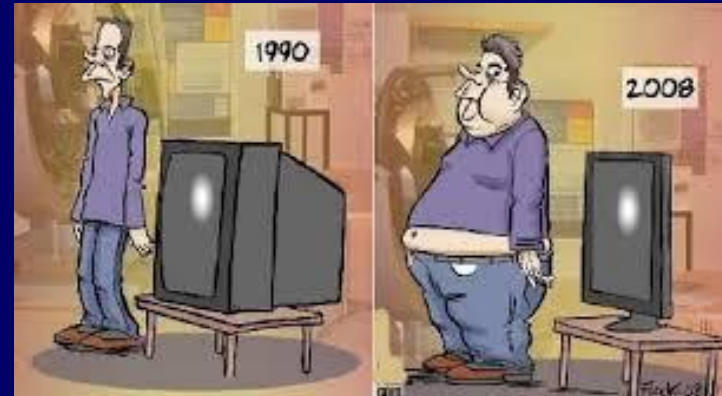




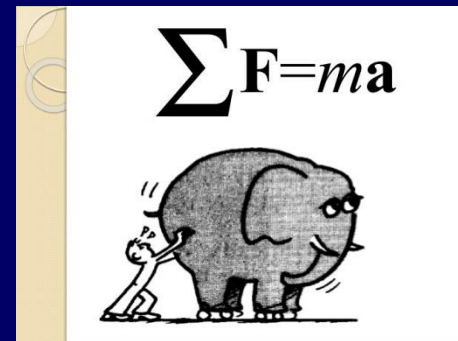
# Geodynamic modelling

## *Basic conservation laws*

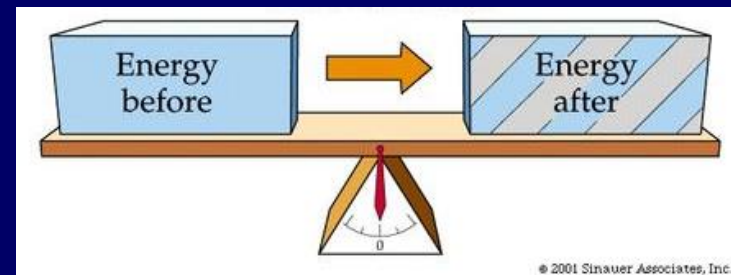
Mass conservation law:



Momentum conservation law:



Energy conservation law:



# Geodynamic modelling

## *Basic conservation laws*

Mass conservation law:

$$\frac{1}{K} \frac{DP}{Dt} - \alpha \frac{DT}{Dt} + \frac{\partial v_i}{\partial x_i} = 0$$

Momentum conservation law:

$$-\frac{\partial P}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} + \rho g_i = \rho \frac{Dv_i}{Dt}$$

Energy conservation law:

$$\rho C_p \frac{DT}{Dt} = \frac{\partial}{\partial x_i} \left( \lambda \frac{\partial T}{\partial x_i} \right) + \frac{1}{\eta_{eff}} \tau_{ij} \tau_{ij} + \rho A + \Delta H_{chem}$$

# Geodynamic modelling

## *Basic conservation laws*

Mass conservation law:

1 equation

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Momentum conservation law:

3 equations

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# Geodynamic modelling

## *Basic conservation laws*

Mass conservation law:

1 equation

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Momentum conservation law:

**Only 5 equations for 11 unknowns!**

3 equations

$$-\frac{\partial p}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} + \rho g_i = \rho \frac{Dv_i}{Dt}$$

Energy conservation law:

1 equation

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# Geodynamic modelling

## *Rheological (constitutive) equations*

Equation of state for density:

1 equation

$$\rho = F(P, T)$$

Deformation mechanisms:

5 equations

$$\dot{\epsilon}_{ij} = \frac{1}{2} \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right) = \Phi(P, T, \tau_{ij})$$

# Geodynamic modelling

## *Rheological (constitutive) equations*

Equation of state for density:

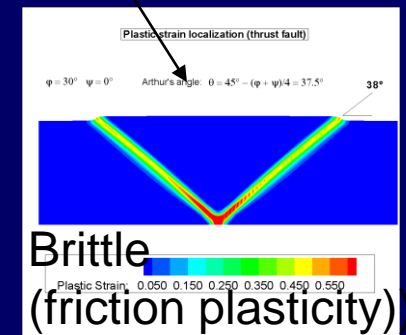
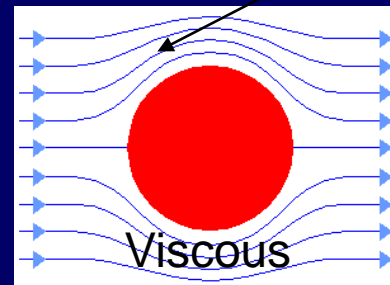
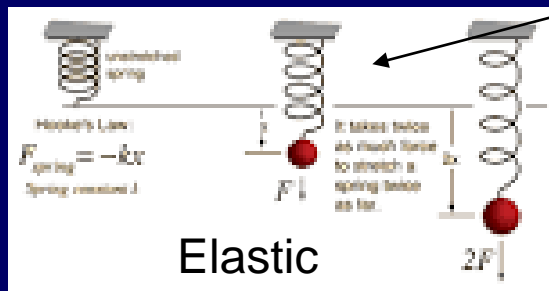
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# Major numerical challenges

Handle large non-linearity

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Handle extreme variations of viscosity  $>5$   
orders of magnitude



# Major numerical challenges

Handle large non-linearity

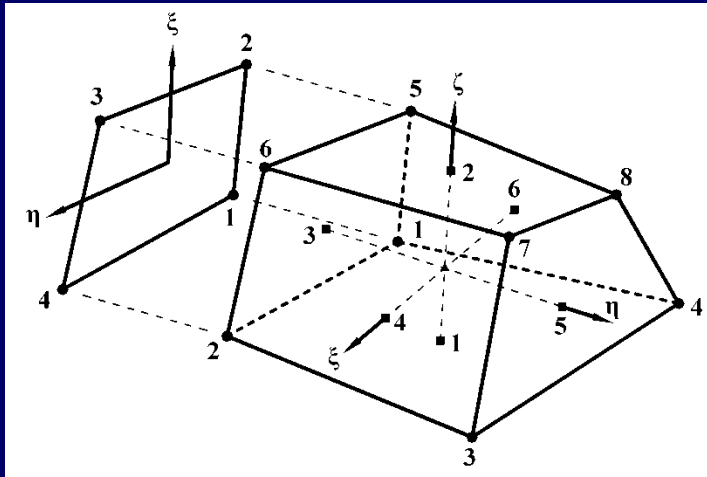
Handle extreme variations of viscosity  $>5$   
orders of magnitude

Model strong strain localization = faults

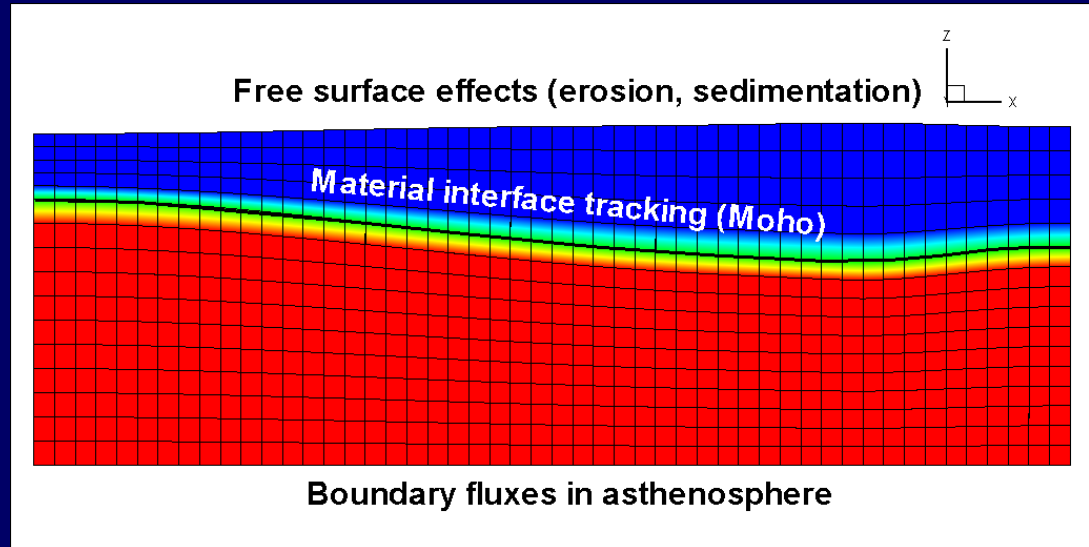
# Numerical methods

# Numerical FE code SLIM3D

Discretization by  
Finite Element Method



Arbitrary Lagrangian-Eulerian  
kinematical formulation



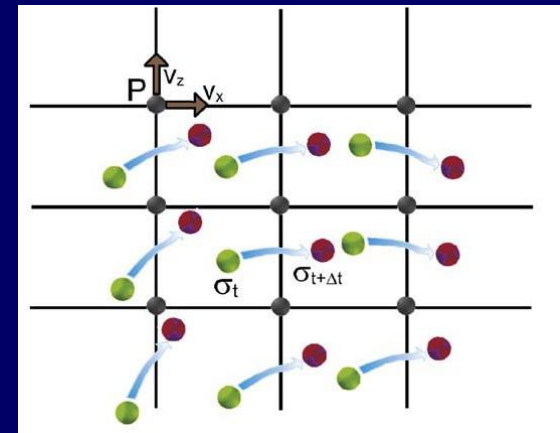
Fast implicit time stepping  
+ Newton-Raphson solver

$$\mathbf{u}_{k+1} = \mathbf{u}_k - \mathbf{K}_k^{-1} \mathbf{r}_k$$

$\mathbf{r}$  — Residual Vector

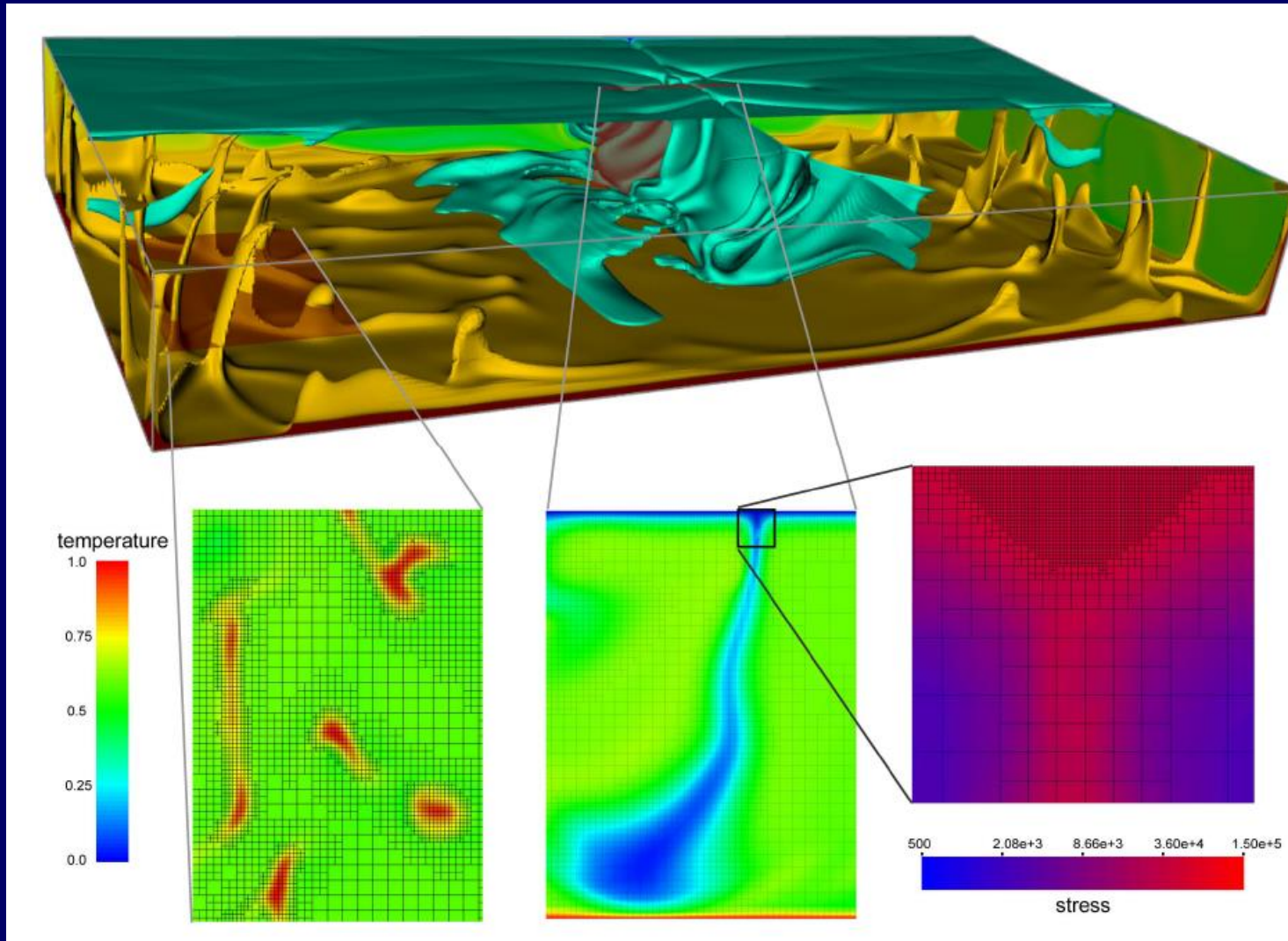
$$\mathbf{K} = \frac{\partial \mathbf{r}}{\partial \Delta \mathbf{u}} \text{ — Tangent Matrix}$$

Remapping of  
entire fields by  
Particle-In-Cell  
technique



Popov and Sobolev (2008)

# Numerical FE code ASPECT

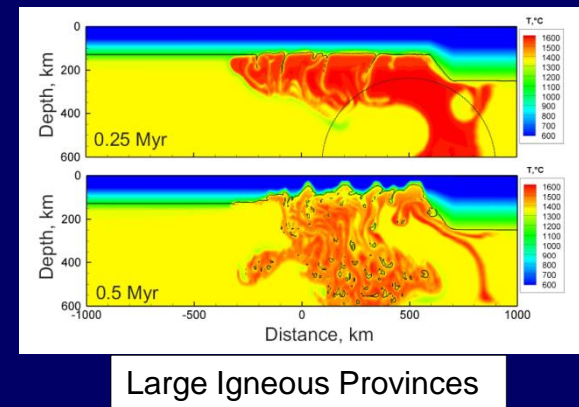
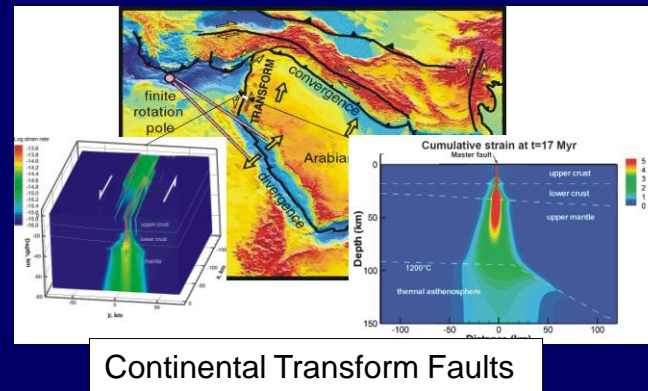
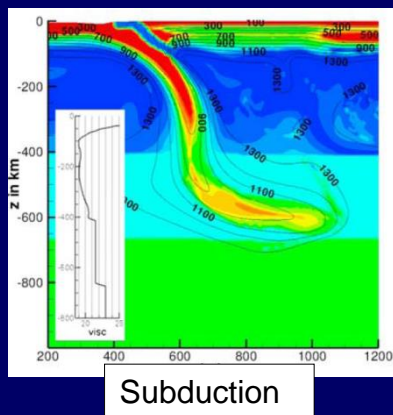
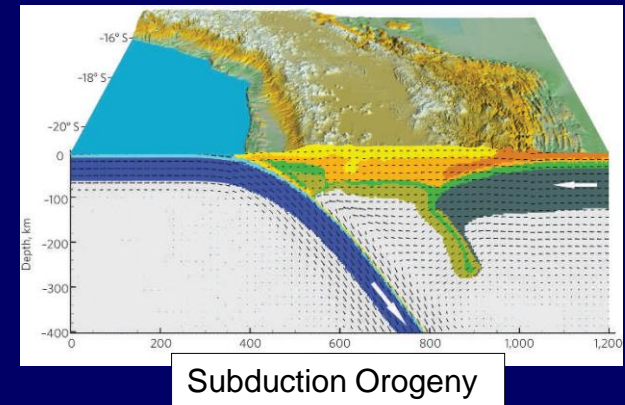
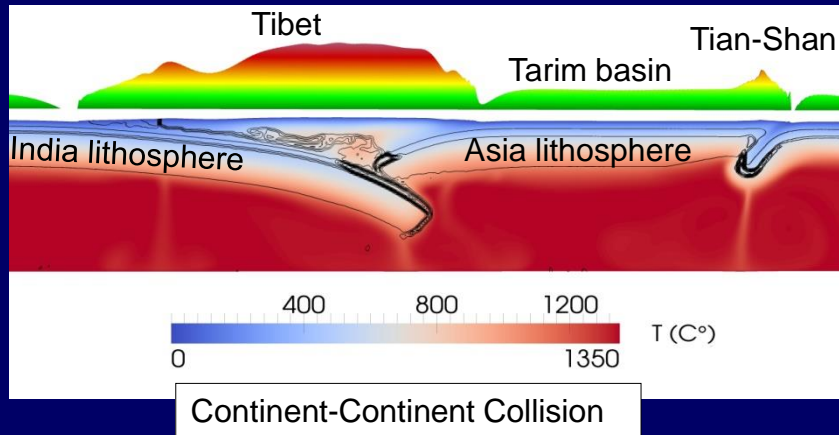


Burstedde et al., 2008-2010

# Section on Geodynamic Modeling at GFZ

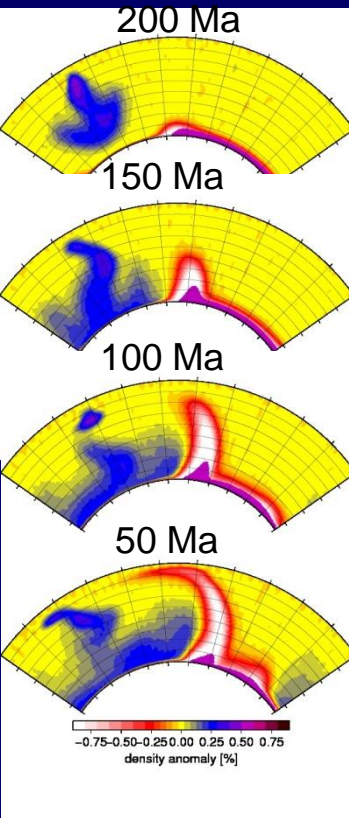
# Lithospheric-scale modeling

Modeling key geodynamic processes constrained by observations

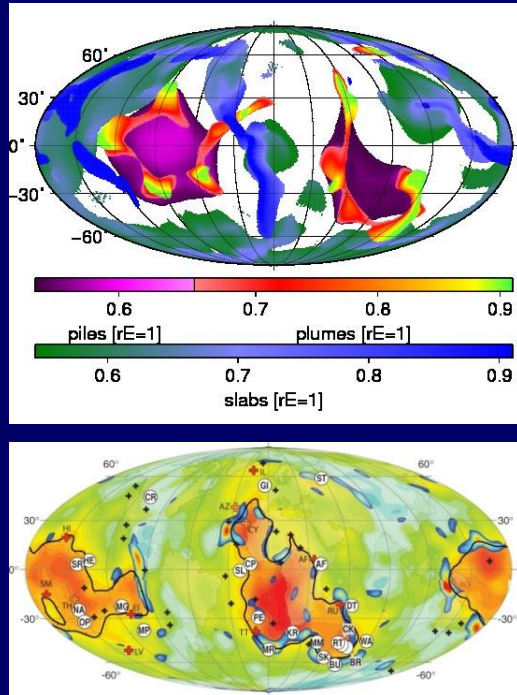


# Global-scale modeling

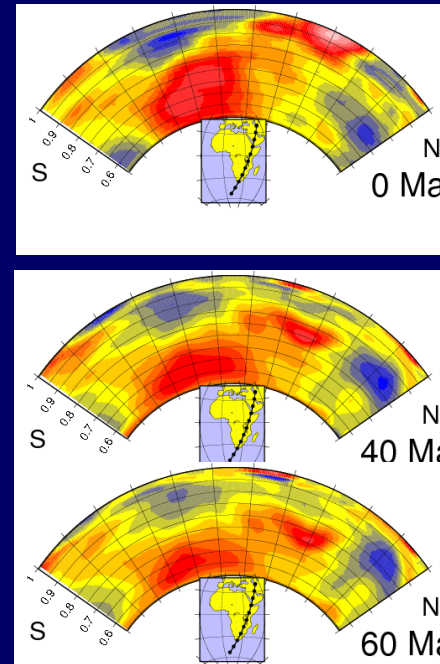
## Reconstructing Earth's mantle through geologic time



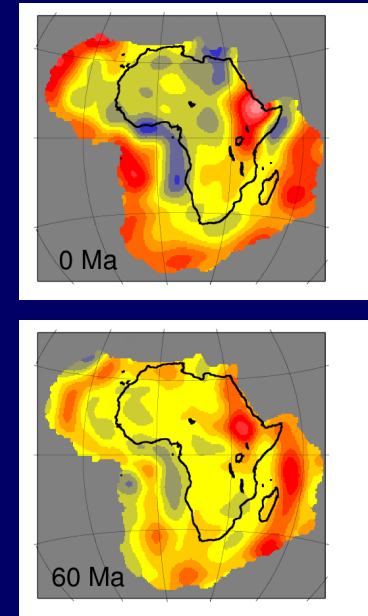
Forward modeling based on subduction history



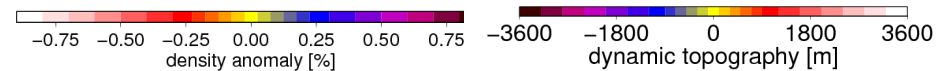
Backward models based on seismic tomography



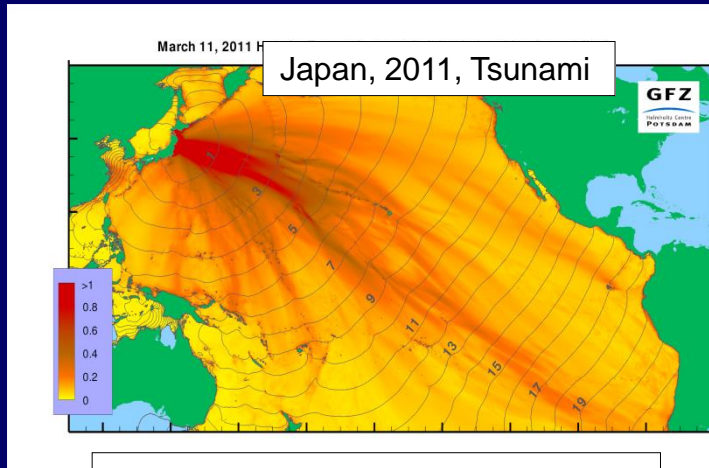
Predicted uplift and subsidence at moving plate



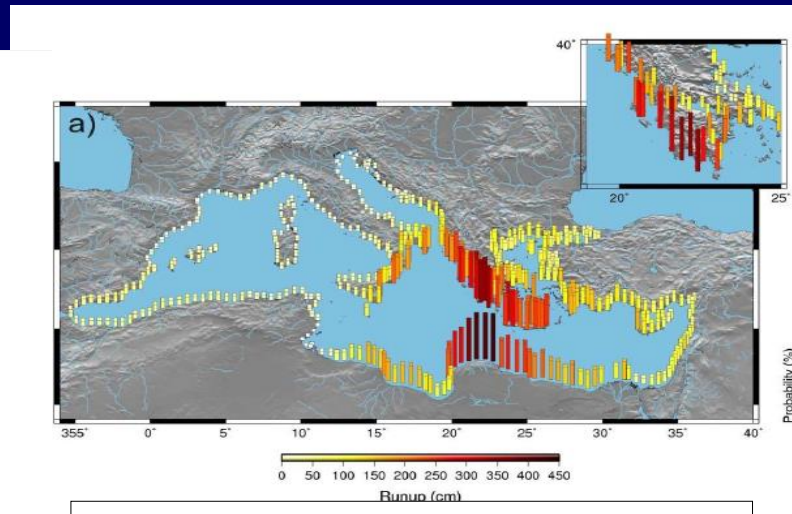
Model and observations: Plumes generated At the margins of thermo-chemical piles



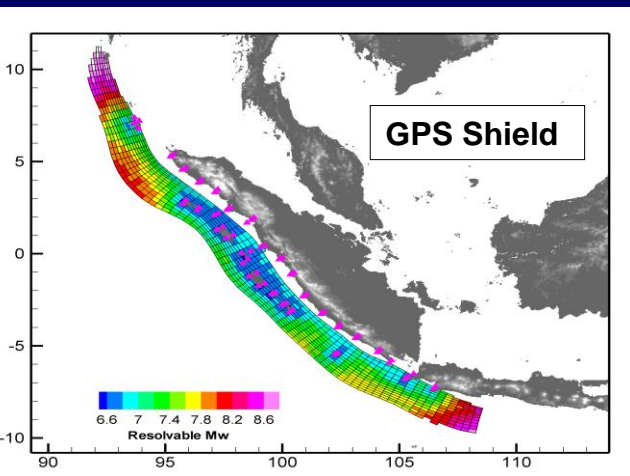
# Link to surface processes



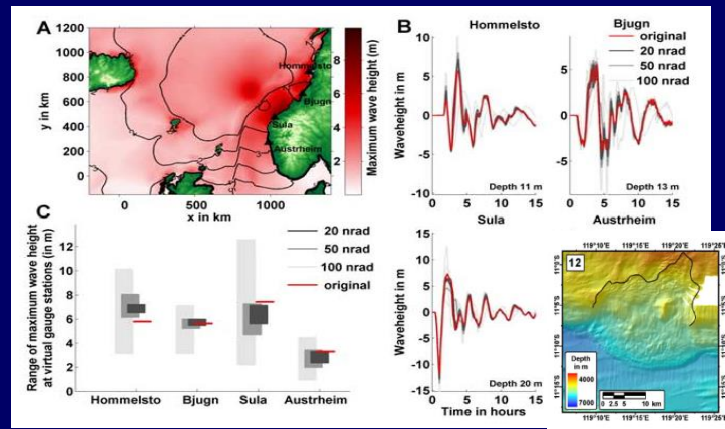
Tsunami and source modeling



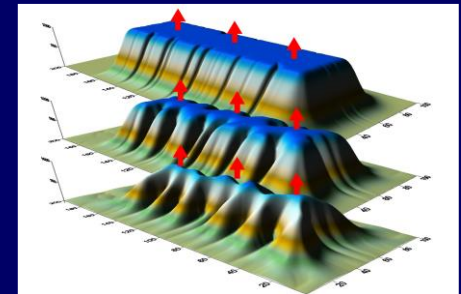
Probabilistic tsunami hazard in Mediterranean



GPS arrays for quick source inversion



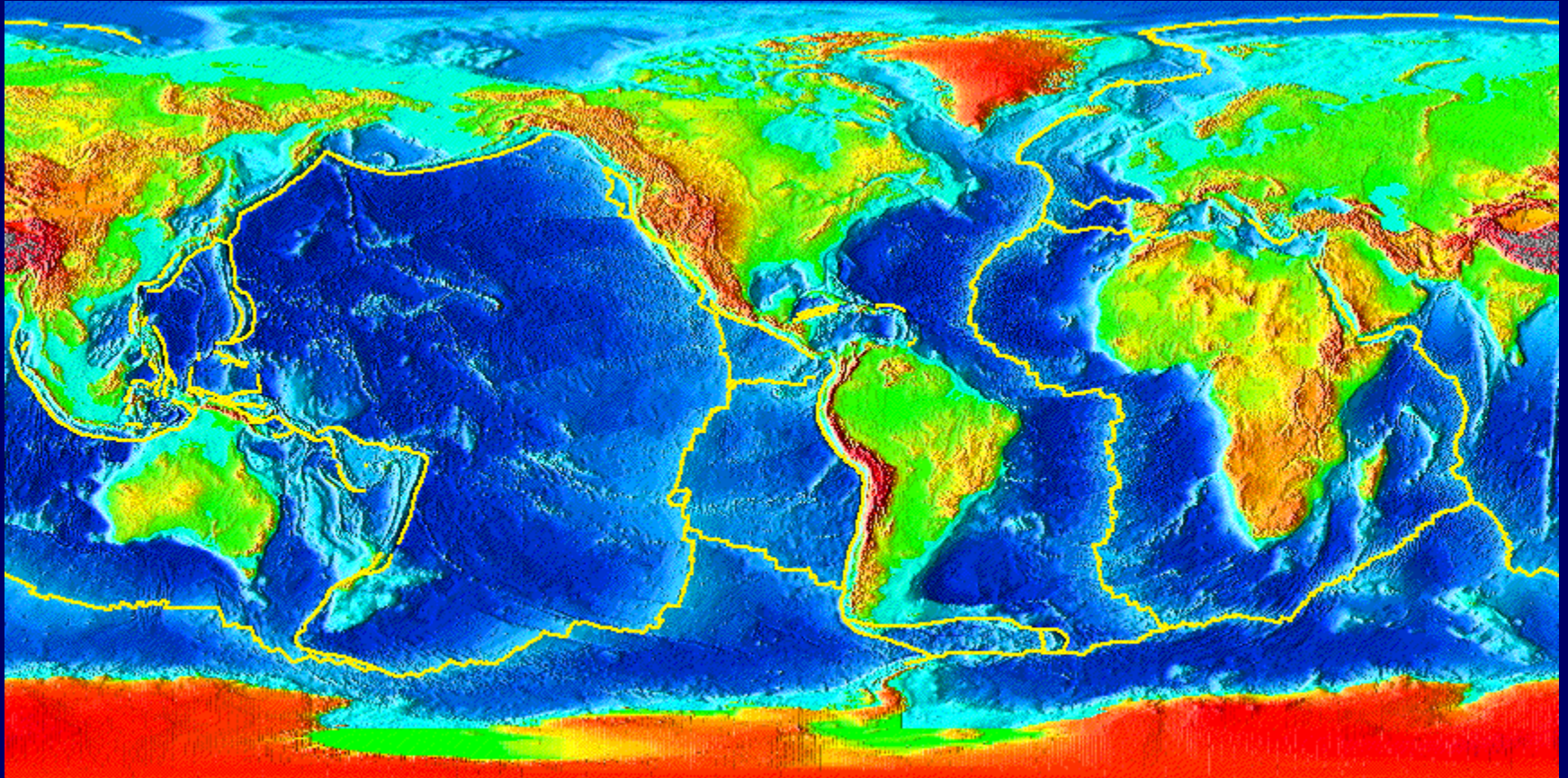
Landslide hazard evaluation and detection



3D Tectonics and erosion



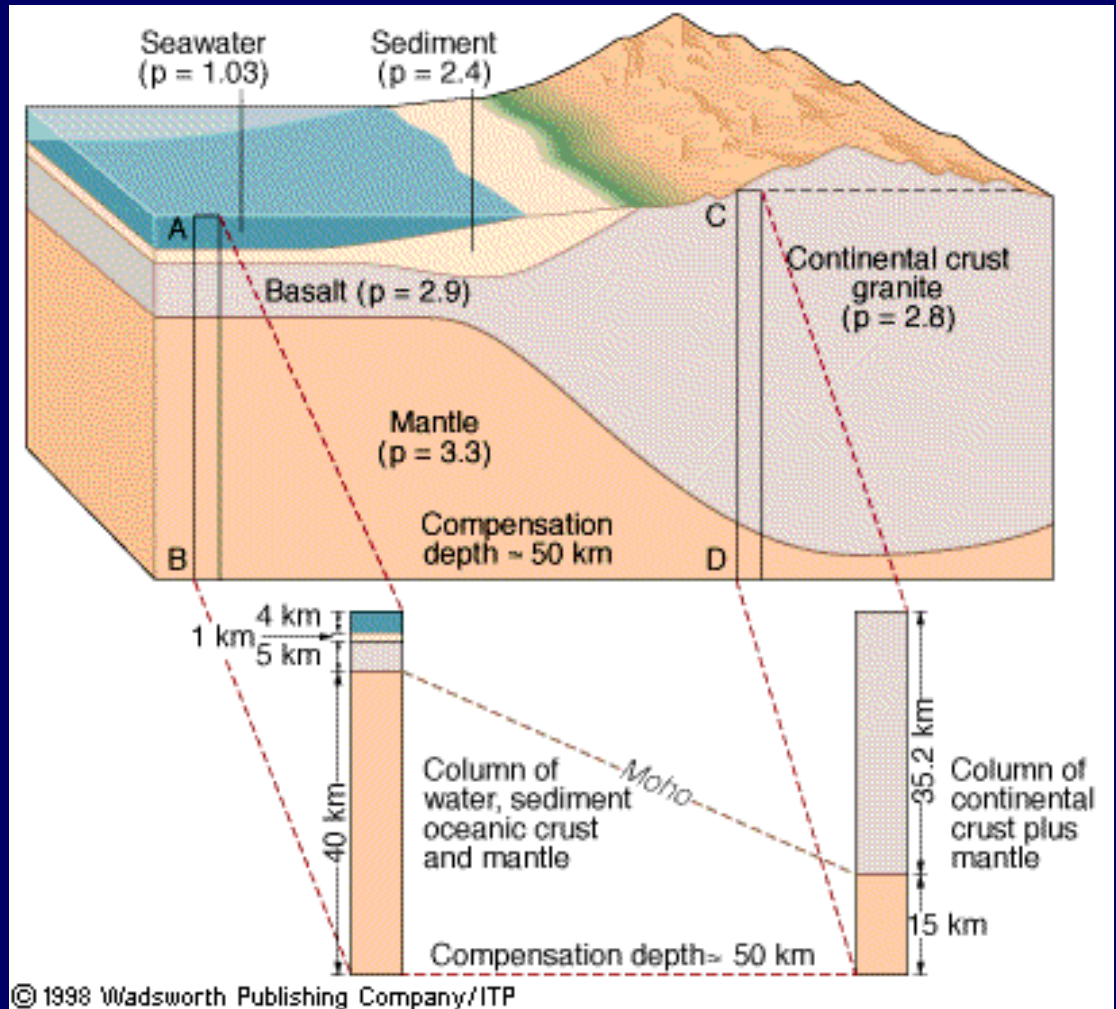
# Why continents?



Crustal Plate Boundaries

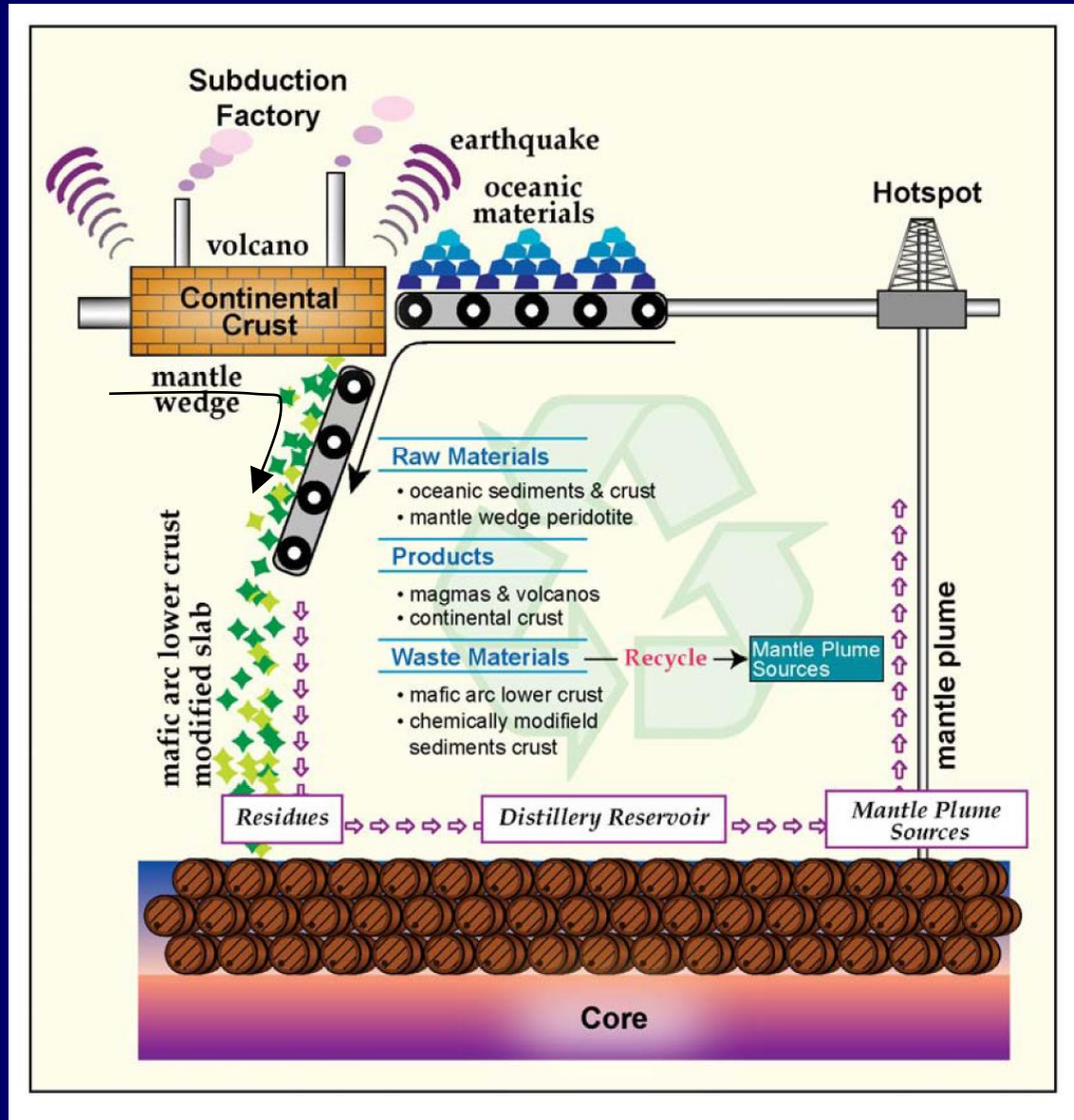
oceanic crust:  
mafic; denser  
continental crust:  
felsic; less dense

*isostasy*:  
columns of mass must be  
the same at a certain  
depth (compensation  
depth) ~ 50 km

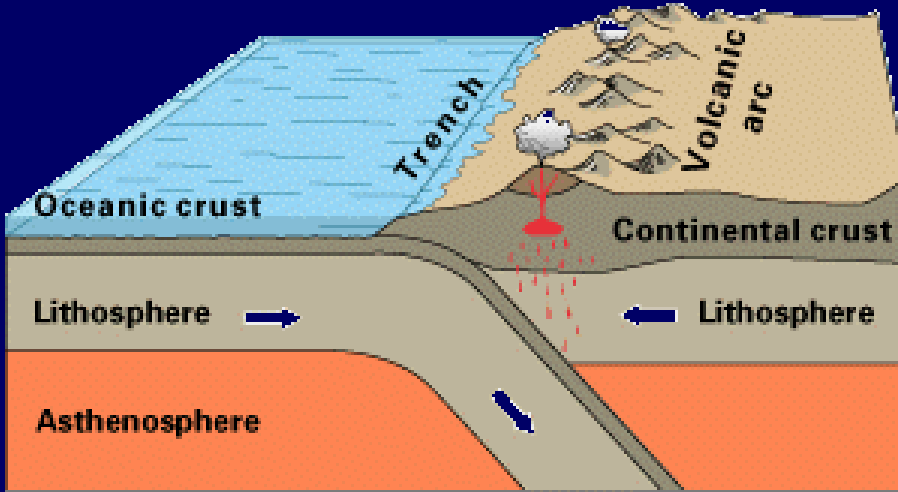


continents have roots  
and stick-up

# Making continental crust

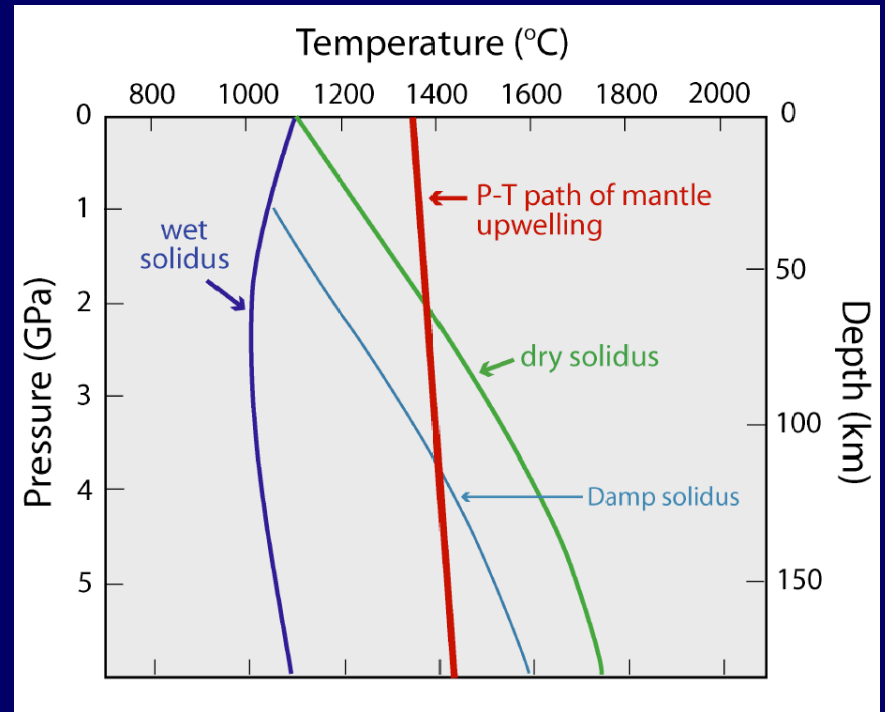


# Subduction zone



Because of water

Why volcanoes?



# Key factors to make continental crust

1. Permanent inflow of fluids, sediments and oceanic crust
2. Melting of mantle rocks enabled by water-rich fluid
3. Permanent inflow of „fresh“ mantle material = corner flow

# Temperature and velocity fields in corner-flow

(Sobolev et al., 2006)

Time, Myr 1.00

## Why corner-flow?

